Transit Searches: Technique
The “Transit” Method

Viewing angle ~ orbital plane!

Delta L / L ~ \(( R_{\text{planet}} / R_{\text{star}})^2\)

Jupiter: ~ 1-2 %

Earth: ~ 0.0084 %
Planet Transits:

Three parameters describe the characteristics of a transit:
• the period of recurrence of the transit;
• the fractional change in brightness of the star, and
• the duration of the transit.
What are Transits and why are they important?

The drop in intensity is given by the ratio of the cross-section areas:

\[ \Delta I = \left( \frac{R_p}{R_*} \right)^2 = \left( \frac{0.1 R_{\text{sun}}}{1 R_{\text{sun}}} \right)^2 = 0.01 \] for Jupiter

Radial Velocity measurements \( \Rightarrow M_p \) (we know \( \sin i \) !)

\[ \Rightarrow \text{mean density of planet} \]

→ Transits allows us to measure the physical properties of the planets
Transit Probability

\[ \sin \theta = \frac{R_*}{a} = |\cos i| \]

a is orbital semi-major axis, and \( i \) is the orbital inclination\(^1\)

\[ P_{\text{orb}} = \int_{90-\theta}^{90+\theta} 2\pi \sin i \, di / 4\pi = \]

\[ -0.5 \cos (90+\theta) + 0.5 \cos(90-\theta) = \sin \theta \]

\[ = \frac{R_*}{a} \text{ for small angles} \]

\(^1\)by definition \( i = 90 \text{ deg} \) is looking in the orbital plane
Note the closer a planet is to the star:

1. The more likely that you have a favorable orbit for a transit
2. The shorter the transit duration
3. Higher frequency of transits (short orbital periods)

→ The transit method is best suited for short period planets.

Prior to 51 Peg it was not really considered a viable detection method.
### Planet Transits

<table>
<thead>
<tr>
<th>Planet</th>
<th>Orbital Period (years)</th>
<th>Semi-Major Axis (A.U.)</th>
<th>Transit Duration (hours)</th>
<th>Transit Depth (%)</th>
<th>Geometric Probability (%)</th>
<th>Inclination Invariant Plane (deg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mercury</td>
<td>0.241</td>
<td>0.39</td>
<td>8.1</td>
<td>0.0012</td>
<td>1.19</td>
<td>6.33</td>
</tr>
<tr>
<td>Venus</td>
<td>0.615</td>
<td>0.72</td>
<td>11.0</td>
<td>0.0076</td>
<td>0.65</td>
<td>2.16</td>
</tr>
<tr>
<td>Earth</td>
<td>1.000</td>
<td>1.00</td>
<td>13.0</td>
<td>0.0084</td>
<td>0.47</td>
<td>1.65</td>
</tr>
<tr>
<td>Mars</td>
<td>1.880</td>
<td>1.52</td>
<td>16.0</td>
<td>0.0024</td>
<td>0.31</td>
<td>1.71</td>
</tr>
<tr>
<td>Jupiter</td>
<td>11.86</td>
<td>5.20</td>
<td>29.6</td>
<td>1.01</td>
<td>0.089</td>
<td>0.39</td>
</tr>
<tr>
<td>Saturn</td>
<td>29.5</td>
<td>9.5</td>
<td>40.1</td>
<td>0.75</td>
<td>0.049</td>
<td>0.87</td>
</tr>
<tr>
<td>Uranus</td>
<td>84.0</td>
<td>19.2</td>
<td>57.0</td>
<td>0.135</td>
<td>0.024</td>
<td>1.09</td>
</tr>
<tr>
<td>Neptune</td>
<td>164.8</td>
<td>30.1</td>
<td>71.3</td>
<td>0.127</td>
<td>0.015</td>
<td>0.72</td>
</tr>
</tbody>
</table>

Finding Earths via transit photometry is very difficult! (But we have the technology to do it from space: Kepler)
Making contact:

1. First contact with star
2. Planet fully on star
3. Planet starts to exit
4. Last contact with star

Note: for grazing transits there is no 2nd and 3rd contact
Shape of Transit Curves

HST light curve of HD 209458b

A real transit light curve is **not** flat
To probe limb darkening in other stars, you can use transiting planets. At the limb the star has less flux than expected, thus the planet blocks less light.
To model the transit light curve and derive the true radius of the planet you have to have an accurate limb darkening law.

Problem: Limb darkening is only known very well for one star – the Sun!
Grazing eclipses/transits

These produce a "V-shaped" transit curve that are more shallow

Planetary hunters like to see a flat part on the bottom of the transit
Probability of detecting a transit $P_{\text{tran}}$

$$P_{\text{tran}} = P_{\text{orb}} \times f_{\text{planets}} \times f_{\text{stars}} \times \Delta T/P$$

$P_{\text{orb}} = \text{probability that orbit has correct orientation}$

$f_{\text{planets}} = \text{fraction of stars with planets}$

$f_{\text{stars}} = \text{fraction of suitable stars (Spectral Type later than F5)}$

$\Delta T/P = \text{fraction of orbital period spent in transit}$
E.g. a field of 10,000 Stars the number of expected transits is:

\[ N_{\text{transits}} = (10,000)(0.1)(0.01)(0.3) = 3 \]

Probability of a transiting Hot Jupiter

Frequency of Hot Jupiters

Fraction of stars with suitable radii

So roughly 1 out of 3000 stars will show a transit event due to a planet. And that is if you have full phase coverage!

CoRoT: looks at 10,000-12,000 stars per field and is finding on average 3 Hot Jupiters per field. Similar results for Kepler

Note: Ground-based transit searches are finding hot Jupiters 1 out of 30,000 – 50,000 stars → less efficient than space-based searches
Catching a transiting planet is thus like playing in the lottery. To win you have to:

1. Buy lots of tickets → Look at lots of stars
2. Play often → observe as often as you can

The obvious method is to use CCD photometry (two dimensional detectors) that cover a large field.

The Instrument Question:
CCD Photometry

CCD Imaging photometry is at the heart of any transit search program

- Aperture photometry
- PSF photometry
- Difference imaging
Aperture Photometry

Magnitude = constant $-2.5 \times \log [\Sigma (\text{data} - \text{sky})/(\text{exposure time})]$.

Instrumental magnitude can be converted to real magnitude by looking at standard stars.
Aperture photometry is useless for crowded fields
PSF: Image produced by the instrument + atmosphere = point spread function

Most photometric reduction programs require modeling of the PSF
Smooth your reference profile with a new profile. This should look like your observation.

Reference profile: e.g. Observation taken under excellent conditions

In a perfect world if you subtract the two you get zero, except for differences due to star variability.
These techniques are fine, but what happens when some light clouds pass by covering some stars, but not others, or the atmospheric transparency changes across the CCD?

You need to find a reference star with which you divide the flux from your target star. *But what if this star is variable?*

In practice each star is divided by the sum of all the other stars in the field, i.e. each star is referenced to all other stars in the field.

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T: Target, Red:
Reference Stars

T/A = Constant
T/B = Constant
T/C = variations
C is a variable star
```
Sources of Errors

Sources of photometric noise:

1. Photon noise:
   
   error = $\sqrt{N_s}$ ($N_s$ = photons from source)
   
   Signal to noise (S/N) ratio = $N_s / \sqrt{N_s} = \sqrt{N_s}$
   
   Root mean square (rms) in brightness = $1/(S/N)$
2. Sky:

Sky is bright, adds noise, best not to observe under full moon or in downtown Austin.

\[ N_{\text{data}} = \text{counts from star} \]
\[ N_{\text{sky}} = \text{background} \]

Error = \( (N_{\text{data}} + N_{\text{sky}})^{1/2} \)
\[ S/N = (N_{\text{data}})/(N_{\text{data}} + N_{\text{sky}})^{1/2} \]
\[ \text{rms scatter} = 1/(S/N) \]

To search for really small transit signals one needs to go to space (CoRoT, Kepler)
3. Dark Counts and Readout Noise:

Dark: Electrons dislodged by thermal noise, typically a few per hour.

This can be neglected unless you are looking at very faint sources.

Readout Noise: Noise introduced in reading out the CCD:

Typical CCDs have readout noise counts of $3-11 \, e^{-1}$ (photons)
Sources of Errors

4. Scintillation Noise:

Amplitude variations due to Earth’s atmosphere

$$\sigma \sim [1 + 1.07(\kappa D^2/4L)^{7/6}]^{-1}$$

D is the telescope diameter
L is the length scale of the atmospheric turbulence
Star looks fainter

Star looks brighter
Sources of Errors

5. Atmospheric Extinction

Atmospheric Extinction can affect colors of stars and photometric precision of differential photometry since observations are done at different air masses, can even produce false detections.

Major sources of extinction:

- Rayleigh scattering: cross section $\sigma$ per molecule $\propto \lambda^{-4}$
Sources of Errors

6. Stellar Variability: Signal that is noise for our purposes

Stellar activity, oscillations, and other forms of variability can hinder one’s ability to detect transit events due to planets.

e.g. sunspots can cause a variations of about 0.1-1%

Fortunately, most of these phenomena have time scales different from the transit periods.
Finding Transits in the Data

1. Produce a time series light curve of your observations using your favorite technique (aperture, psf, or difference imaging photometry)

Fig. 2. Pre-processed and normalised white light curve of CoRoT-exo-4.
Finding Transits in the Data

2. Remove the bumps and wiggles due to instrumental effects and stellar variability using high pass filters
Finding Transits in the Data

3. Phase fold the data using a trial period
Finding Transits in the Data

3. Perform a least squares fit using a box (BLS = box least squares)

Find the best fit box of width, $w$, and depth $d$.

Define a frequency spectrum of residuals (parameter of best fit) as a function of trial periods. Peaks occur at most likely values of transit periods. The BLS is the most commonly used transit algorithm.
Confirming Transit Candidates

A transit candidate found by photometry is only a candidate until confirmed by spectroscopic measurement (radial velocity).

Radial Velocity measurements are essential for confirming the nature (i.e. get the mass) of the companion, and to exclude so-called false positives.

Current programs are finding transit candidates faster than they can be confirmed bottleneck.
Radial Velocity Curve for HD 209458

Period = 3.5 days
Msini = 0.63 \text{ M}_{\text{Jup}}
False Positives

*It looks like a planet, it smells like a planet, but it is not a planet*

1. Grazing eclipse by a main sequence star:

One should be able to distinguish these from the light curve shape and secondary eclipses, but this is often difficult with low signal to noise.

These are easy to exclude with Radial Velocity measurements as the amplitudes should be tens km/s (2–3 observations).
2. Giant Star eclipsed by main sequence star:

Giant stars have radii of $10 - 100 \, R_\odot$ which translates into photometric depths of $0.0001 - 0.01$ for a companion like the sun.

These can easily be excluded using one spectrum to establish spectral and luminosity class. In principle no radial velocity measurements are required.

Often a giant star can be known from the transit time. These are typically several days long!
3. Eclipsing Binary as a background (foreground) star:

Difficult case. This results in no radial velocity variations as the fainter binary probably has too little flux to be measured by high resolution spectrographs. Large amounts of telescope time can be wasted with no conclusion. High resolution imaging may help to see faint background star.
4. Eclipsing binary in orbit around a bright star (hierarchical triple systems)

Another difficult case. Radial Velocity Measurements of the bright star will show either long term linear trend no variations if the orbital period of the eclipsing system around the primary is long. This is essentially the same as case 3) but with a bound system.
5. Unsuitable transits for Radial Velocity measurements

Transiting planet orbits an early type star with rapid rotation which makes it impossible to measure the RV variations or you need lots and lots of measurements.

Depending on the rotational velocity RV measurements are only possible for stars later than about F3
Example: Results from the CoRoT Initial Run Field

26 Transit candidates:

Grazing Eclipsing Binaries: 9

Background Eclipsing Binaries: 8

Unsuitable Host Star: 3

Unclear (no result): 4

Planets: 2

→ for every „quality“ transiting planet found there are 10 false positive detections. These still must be followed-up with spectral observations
Search Strategies

Look at fields where there is a high density of stars.

**Strategy 1:**
Look in galactic plane with a small (10-20 cm) wide field (> 1 deg$^2$) telescope

Pros: stars with $6 < V < 15$
Cons: Not as many stars
Search Strategies

Strategy 2:
Look at the galactic bulge with a large (1-2m) telescope (e.g. OGLE)
Pros: Potentially many stars
Cons: V-mag > 14 faint!

Image in galactic bulge
Search Strategies

Strategy 3:
Look at clusters with a large (1-2m) telescope

Pros: Potentially many stars (depending on cluster)
Cons: $V$-mag $> 14$ faint! Often not enough stars, most open clusters do not have 3000-10000 stars

Pleiades: open cluster

M 92 globular cluster
Search Strategies

Strategy 4:
One star at a time!

The MEarth project (http://www.cfa.harvard.edu/~zberta/mearth/) uses 8 identical 40 cm telescopes to search for terrestrial planets around M dwarfs one after the other.
Radial Velocity Follow-up for a Hot Jupiter

The problem is not in finding the transits, the problem (bottleneck) is in confirming these with RVs which requires high resolution spectrographs.

<table>
<thead>
<tr>
<th>Telescope</th>
<th>Easy</th>
<th>Challenging</th>
<th>Impossible</th>
</tr>
</thead>
<tbody>
<tr>
<td>2m</td>
<td>$V &lt; 9$</td>
<td>$V = 10-12$</td>
<td>$V &gt; 13$</td>
</tr>
<tr>
<td>4m</td>
<td>$V &lt; 10-11$</td>
<td>$V = 12-14$</td>
<td>$V &gt; 15$</td>
</tr>
<tr>
<td>8–10m</td>
<td>$V &lt; 12-14$</td>
<td>$V = 14-16$</td>
<td>$V &gt; 17$</td>
</tr>
</tbody>
</table>

It takes approximately 8-10 hours of telescope time on a large telescope to confirm one transit candidate.
Summary

1. The Transit Method is an efficient way to find short period planets.

2. Combined with radial velocity measurements it gives you the mass, radius and thus density of planets.

3. Roughly 1 in 3000 stars will have a transiting hot Jupiter → need to look at lots of stars (in galactic plane or clusters).

4. Radial Velocity measurements are essential to confirm planetary nature.

5. A small telescope can do transit work (i.e. even amateurs).