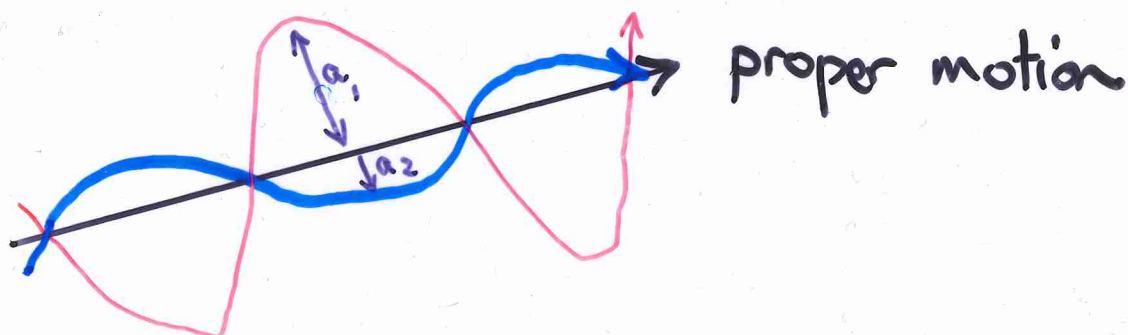


VISUAL BINARIES

- A system in which two stars are resolved by a telescope
- Stars seen to orbit each other but periods are long [WHY?]
 $P \sim 10s \text{ to } 10000 \text{ years}$
- Relative masses, m_1/m_2



STAR 2 more massive than STAR 1 [WHY?]

$$\frac{m_1}{m_2} = \frac{a_2}{a_1}$$

SIRIUS

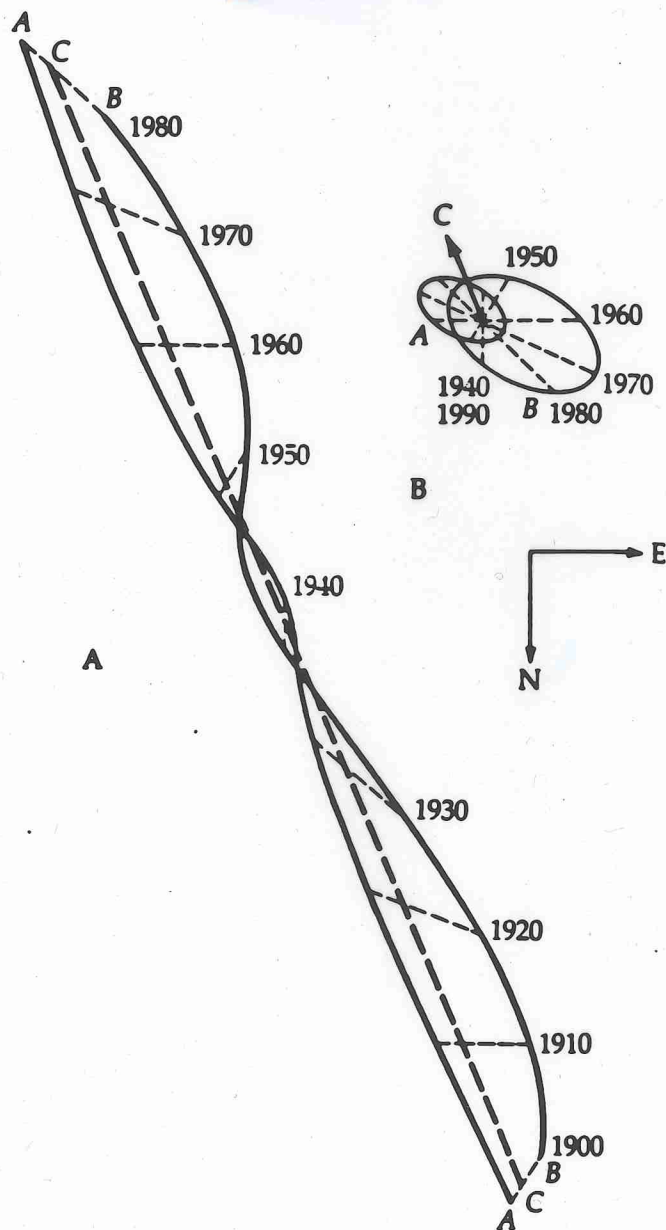
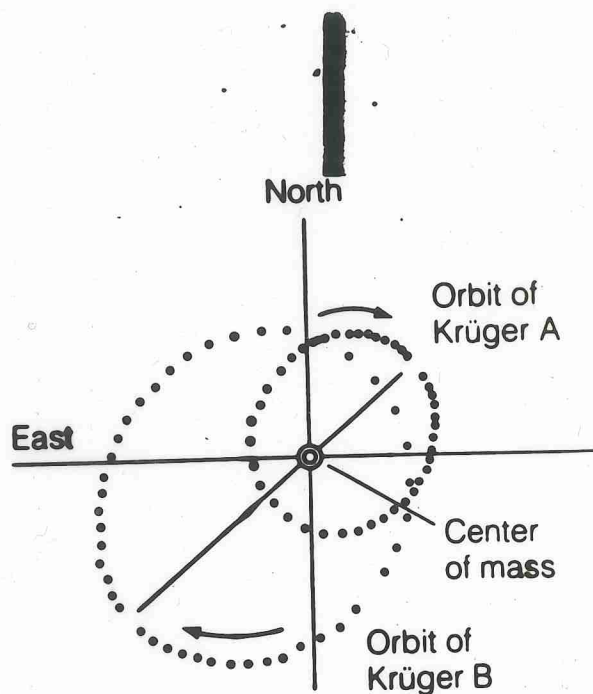
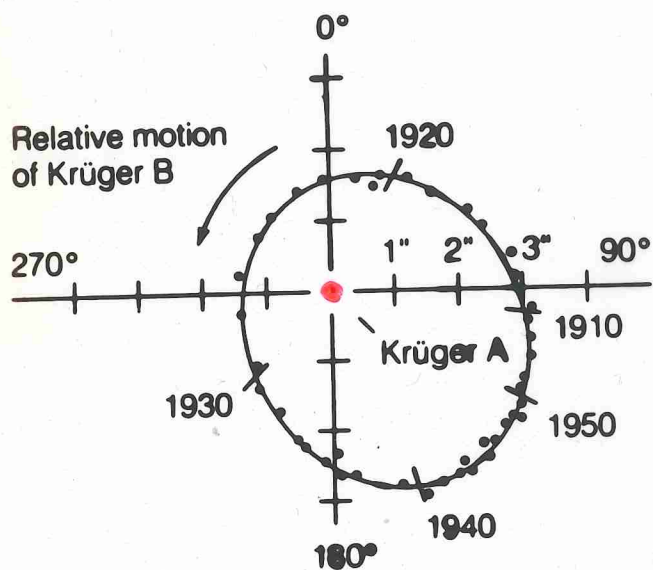


Figure 12-2

Motions of Sirius A and B. (A) The apparent motions relative to background stars of Sirius (A), its companion (B), and the center of mass of the system (C). (B) Orbital motions of Sirius A and B relative to the system's center of mass.



APPARENT RELATIVE
ORBIT

- INDIVIDUAL MASSES, m_1 , & m_2

CORRECT OBSERVED ORBIT FOR
ITS TILT RELATIVE TO LINE
OF SIGHT

DETERMINE PERIOD AND SEMI-MAJOR
AXIS ESTIMATE DISTANCE

APPLY KEPLER'S 3rd LAW !

$$m_1 + m_2 = \frac{a^3}{p^2}$$

TWO EQNS, TWO UNKNOWN

→ m_1 and m_2

VITAL SOURCE OF STELLAR
MASSES

ECLIPSING BINARIES

- Stars experience mutual eclipses:
ORBITS SEEN EDGE-ON

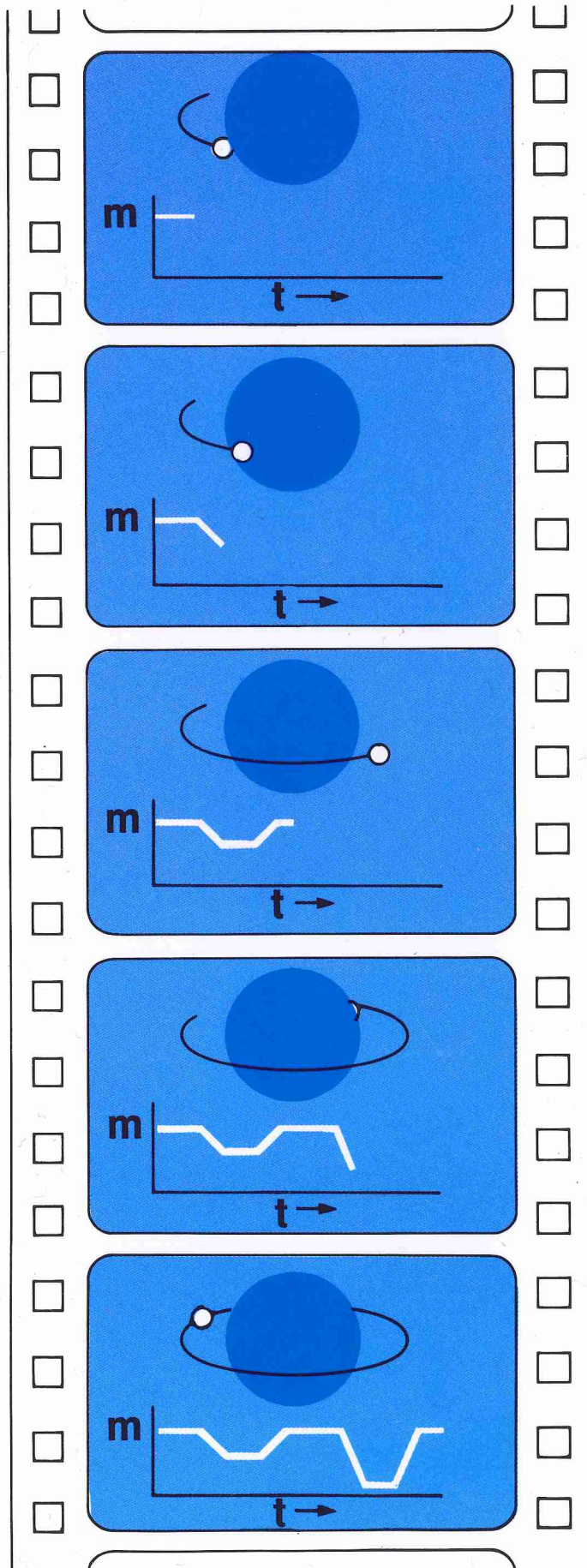
- BRIGHTNESS VARIATIONS/ECLIPSES
and RADIAL VELOCITY VARIATIONS
are observed

→ m_1, m_2 [KEPLER'S LAWS]

R_1, R_2 [ECLIPSE DURATION
+ RADIAL VELOCITY]

ORBIT DIMENSIONS

WHY ARE ECLIPSING BINARIES
NOT VISUAL BINARIES?



Eclipsing binary—changes in brightness

Seeds: Horizons, 1995 ed., Fig. 8-18; Foundations of Astronomy, 1994 ed., Fig. 10-18

SPECTROSCOPIC BINARIES

- A binary system in which stars are too close to be seen as 2 stars but their presence revealed by spectroscopy [Doppler effect]
- If stars have similar luminosities, both contribute to total light.

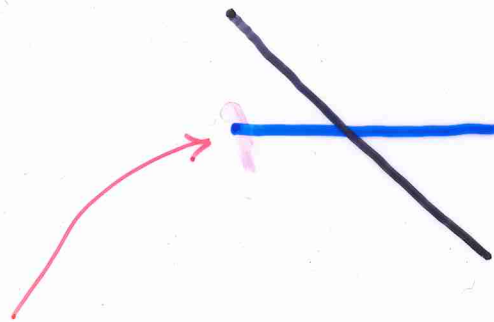
TWO SETS OF ABSORPTION LINES
SEEN : DOUBLE-LINED SB

- If luminosities are dissimilar, one dominates light

ONE SET OF ABSORPTION LINES:
SINGLE-LINED SPECTROSCOPIC BINARY

• RADIAL VELOCITIES measured

CANNOT DETERMINE TRUE SIZE OF ORBITS : TILT TO LINE OF SIGHT IS INDETERMINATE



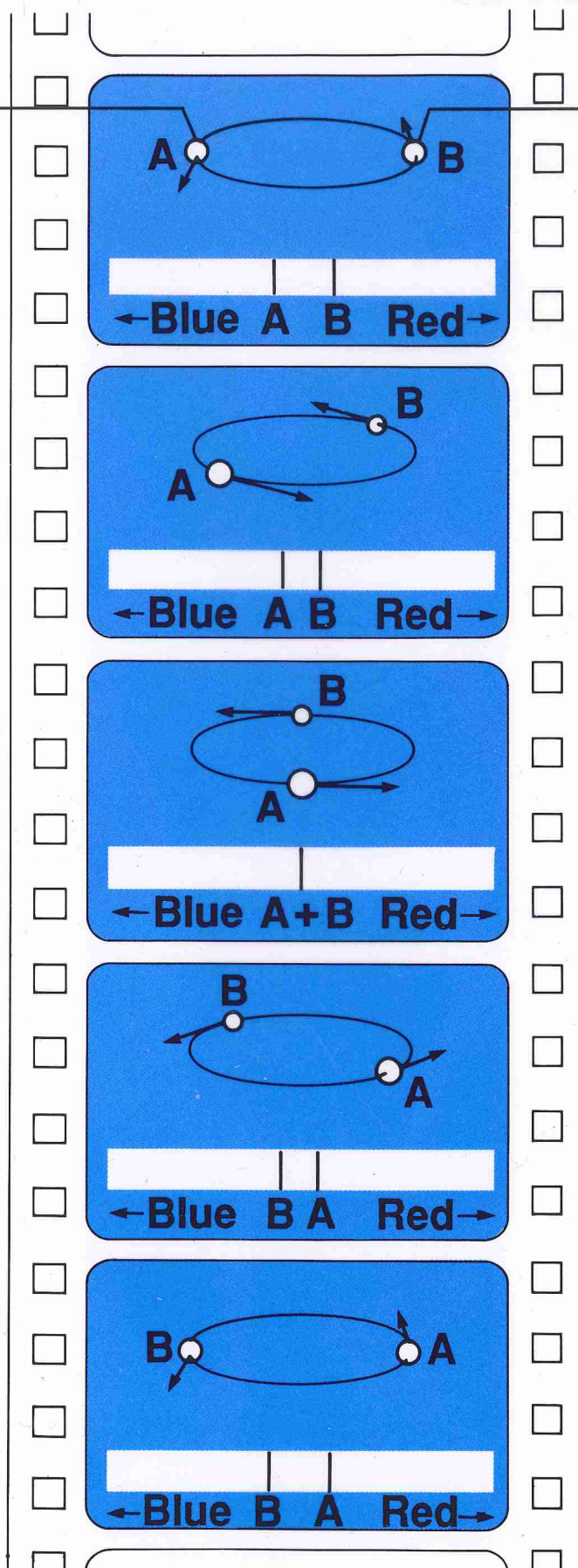
RADIAL VELOCITIES
TELL US THIS PROJECTED
SIZE

(SB2) $\Rightarrow \frac{m_1}{m_2}$ from the amplitudes
of the radial velocity
swings

(SB1) $\Rightarrow$ LOWER LIMIT to
($m_1 + m_2$)

Approaching

Receding



Spectroscopic binary—Doppler shifts

Seeds: Horizons, 1995 ed., Fig. 8-14; Foundations of Astronomy, 1994 ed., Fig. 10-12

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MASS - LUMINOSITY RELATION

- MAIN SEQUENCE STARS

$$L \propto m^4$$

- WHITE DWARFS

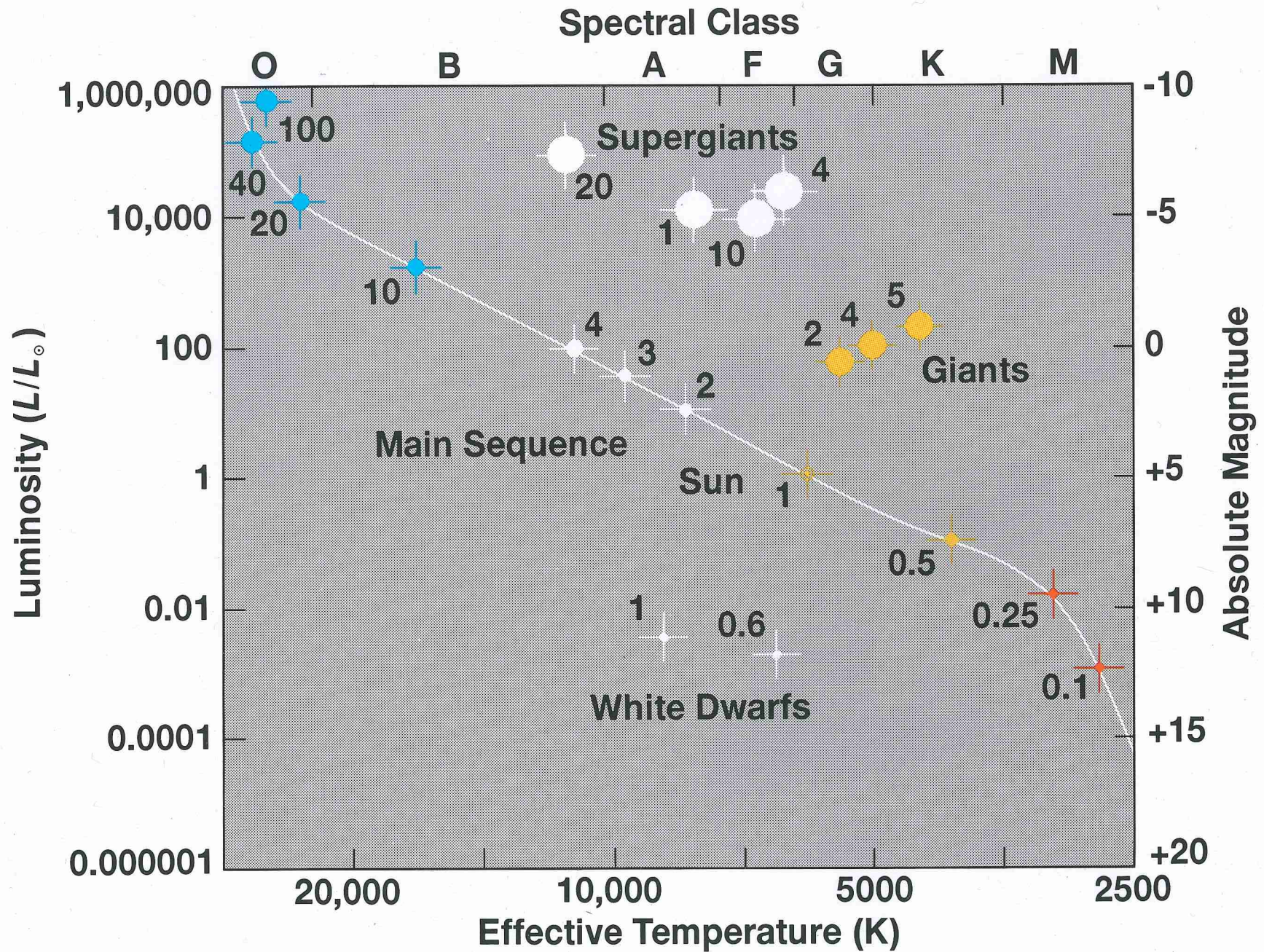
$$m \sim 0.6 m_{\odot}$$

L varies with age

- RED GIANTS

COMPLEX : L-m RELATION

(SEE LATER)



H-R diagram—measured masses of stars

Hartmann/Impey: The Cosmic Journey, 5th ed., Fig. 17-8

STELLAR EVOLUTION

- DIRECTED FROM BIRTH BY GRAVITY (STELLAR MASS)

- POSSIBLE CONCLUSIONS

① GRAVITY WINS : * $\longrightarrow$ BLACK HOLE

② GRAVITY PERMANENTLY THWARTED :

GRAVITY OPPOSED BY A NON-THERMAL PRESSURE

* $\longrightarrow$ STABLE COLD REMNANT

WHITE DWARF

NEUTRON STAR

③ GRAVITY 'LOSES':

STAR EXPLODES, LEAVES NO
REMNANT.

- MASS OF REMNANT IS LESS THAN
INITIAL MASS OF STAR
- VERY LITTLE MASS ($<1\%$) CONVERTED
TO ENERGY
- A LOT OF MASS SHED FROM STAR
DURING ITS EVOLUTION AND AT ITS
DEATH
- EVOLUTION OF STARS IN A BINARY CAN DIFFER
GREATLY FROM SIMILAR SINGLE STARS (MASS
TRANSFERRED BETWEEN STARS)

MAIN SEQUENCE LIFETIMES

$$\text{LIFETIME} = \frac{\text{FUEL SUPPLY}}{\text{RATE OF CONSUMPTION}}$$

SIMPLE ASSUMPTIONS $\rightarrow$

$$t \propto \frac{\text{MASS OF STAR}}{\text{LUMINOSITY OF STAR}} = \frac{m}{L}$$

BUT $L \propto m^4$ FOR MAIN SEQ. STARS

$$t \propto \frac{m}{m^4} = \frac{1}{m^3}$$

$$\frac{t_{*}}{t_{\text{sun}}} = \left(\frac{m_{\text{sun}}}{m_{*}} \right)^3$$

DIFFERENT
L-M → ||

MASS ($M_{\odot}$)	$\frac{L}{L_{\odot}}$	$\frac{t}{t_{\odot}}$	t(yrs)
0.1	1/200	20	200 Billion
0.5	1/16	8	80 Billion
1	1	1	10 Billion
5	625	1/125	80 Million
10	10,000	1/1000	10 Million
50	6,250,000	1/125,000	80,000
100	100 Million	1/1,000,000	10,000

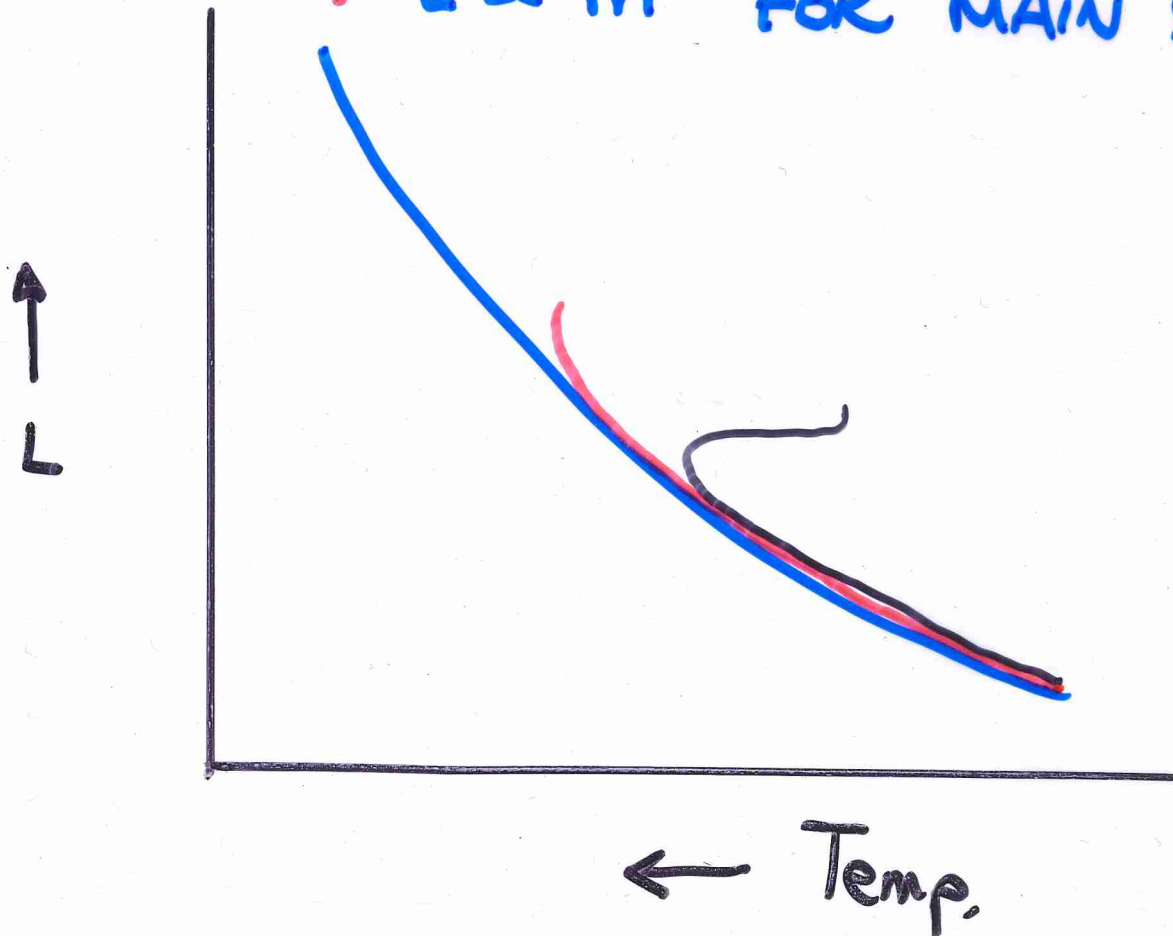
$$L \propto m^4$$

$$t \propto \frac{m}{L} = \frac{m}{m^4} = \frac{1}{m^3}$$

NOTE : ENORMOUS
RANGE

CLUSTER AGES

- KEY POINT: MASSIVE STARS HAVE SHORTER LIFETIMES THAN LESS MASSIVE STARS ($t \propto 1/m^3$)
: $L \propto m^4$ FOR MAIN SEQUENCE



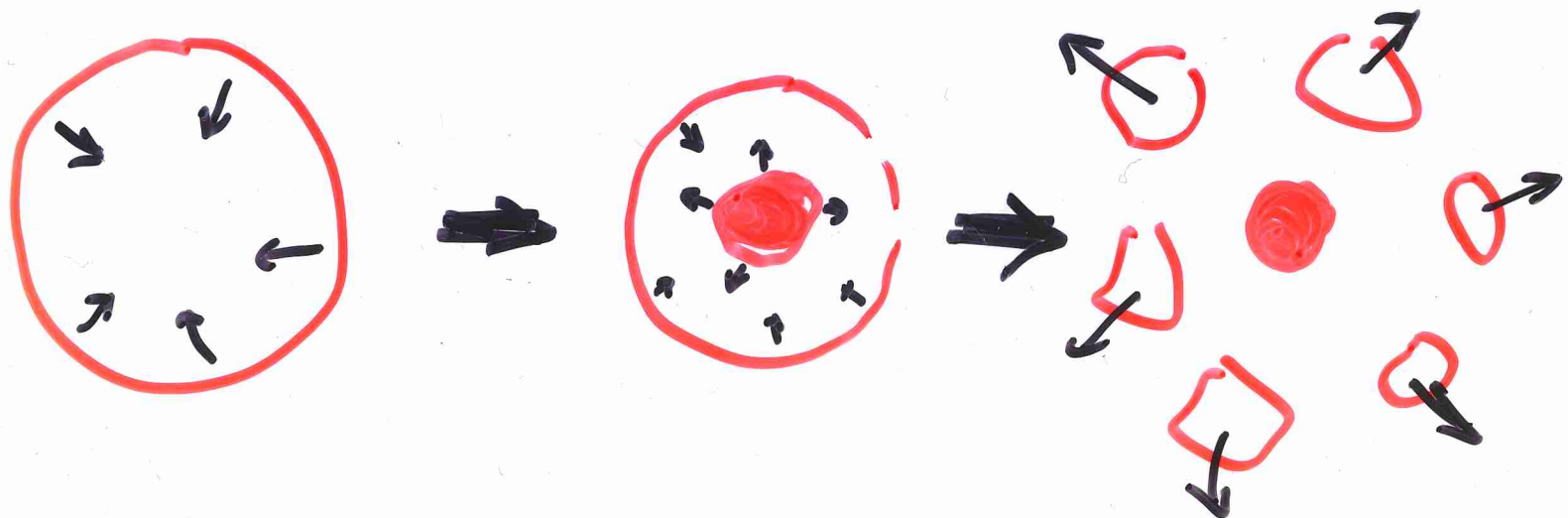
YOUNGEST ?
OLDEST ?

RANGE OF STELLAR MASSES

- **MAXIMUM** $\sim 100 M_{\text{SUN}}$

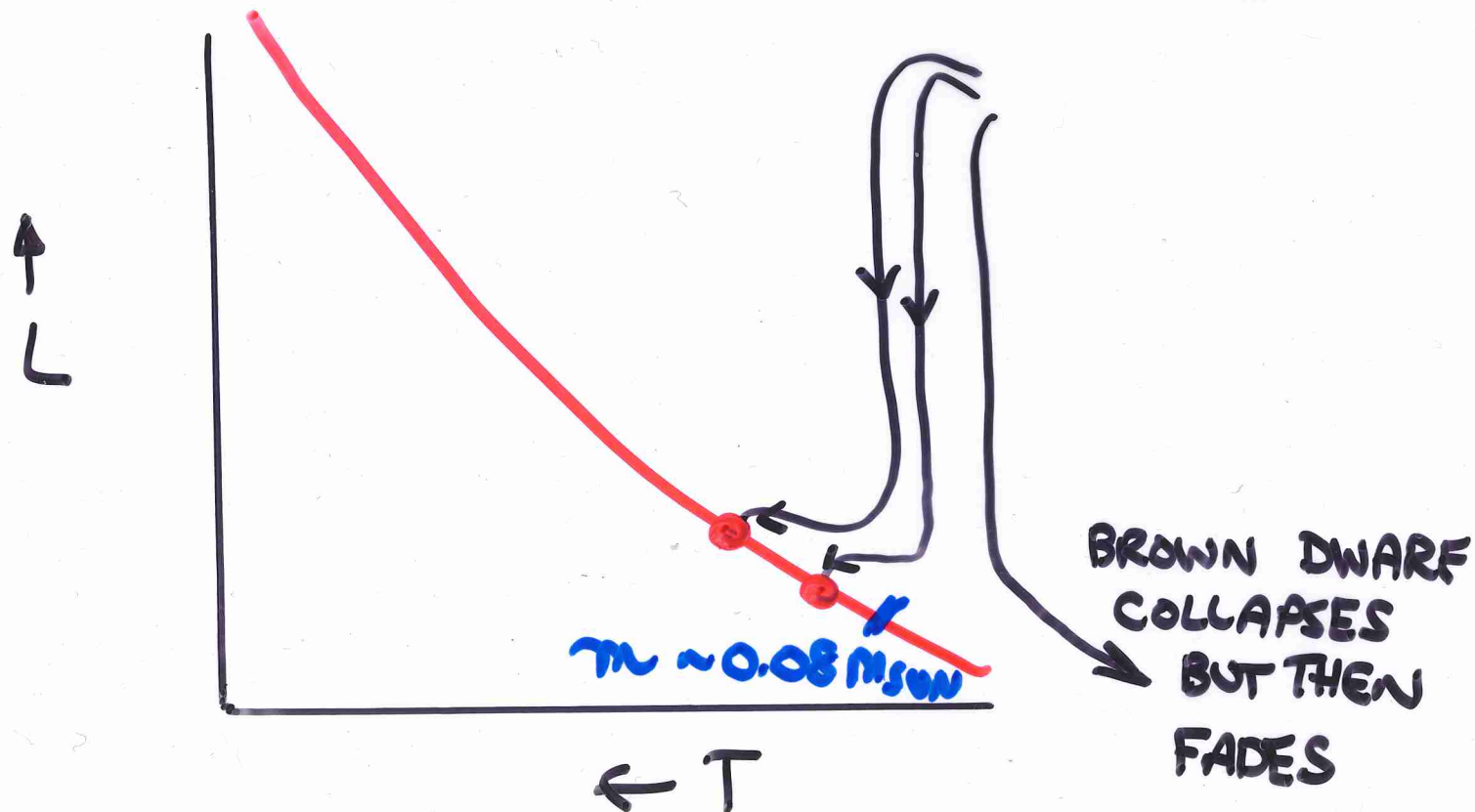
- IF A PROTOSTAR $> 100 M_{\text{SUN}}$ FORMS,
CORE COLLAPSES QUICKLY AND HEATS UP
TO BLOW OFF OUTER LAYERS.

SLIMMED PROTOSTAR $\approx 100 M_{\text{SUN}}$



• MINIMUM $\sim 0.08 M_{\text{sun}}$ SEMANTICS!

A STAR BURNS $4H \rightarrow He$. FOR $M < 0.08 M_{\text{sun}}$,
CORE TEMPERATURE TOO LOW TO BURN H
SUCH OBJECTS ARE CALLED BROWN DWARFS



STAR FORMATION [SEEDS 12-1]

- OCCURS IN COLD DENSE CLOUDS OF GAS

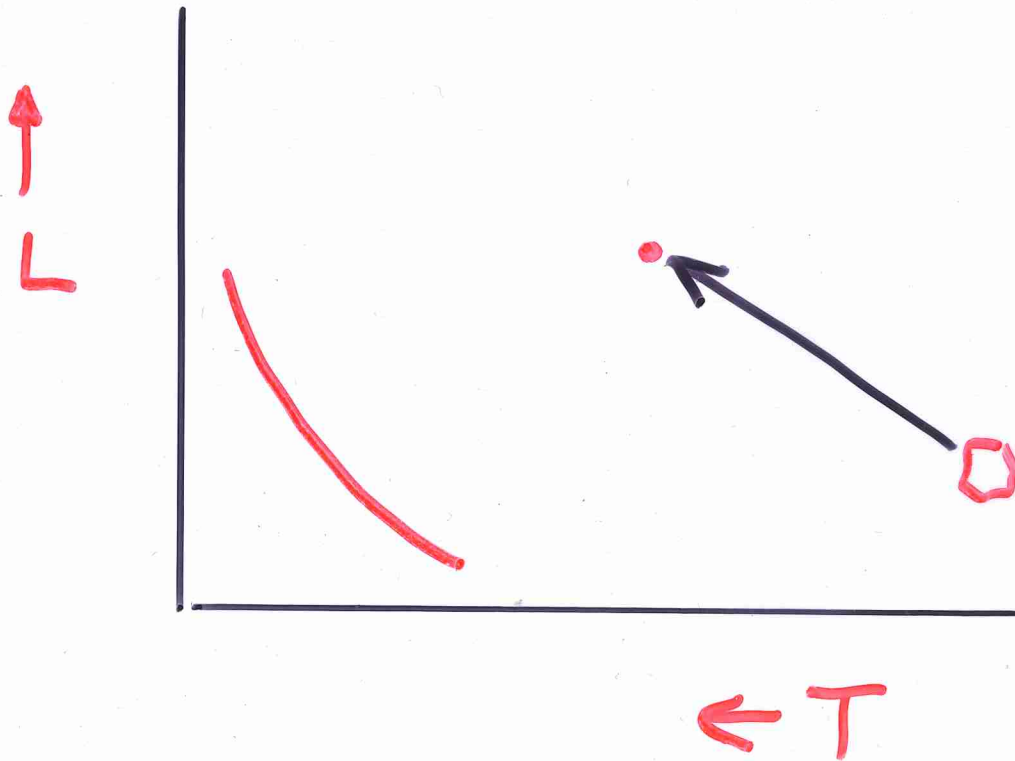
- DIRECTED BY GRAVITY

IF THERMAL PRESSURE IN CLOUD IS TOO LOW TO RESIST GRAVITY, CLOUD BEGINS TO COLLAPSE.

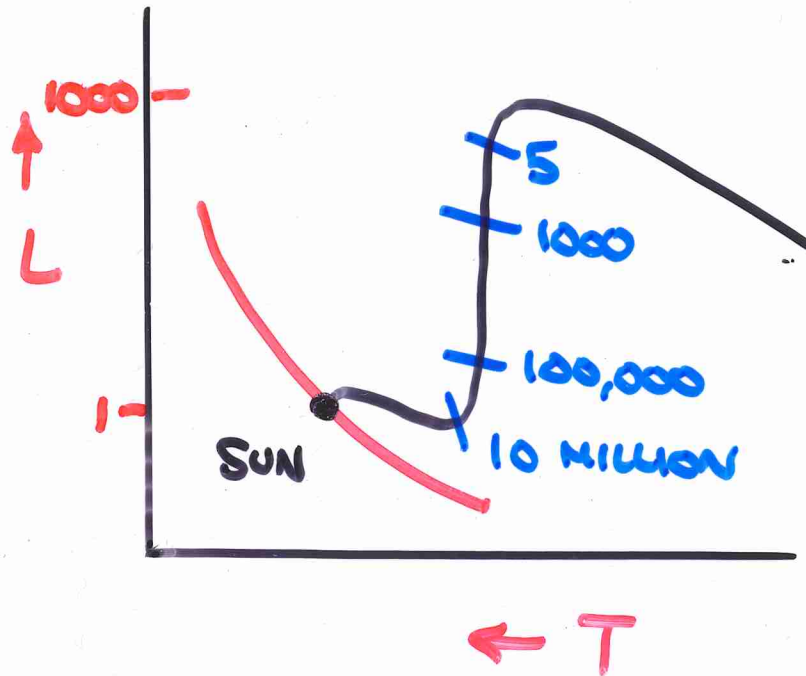
LARGE CLOUDS ($1000^+ m_{\text{sun}}$) COLLAPSE
AND FRAGMENT INTO SMALLER CLOUDS
→ STARS

- EARLY COLLAPSE

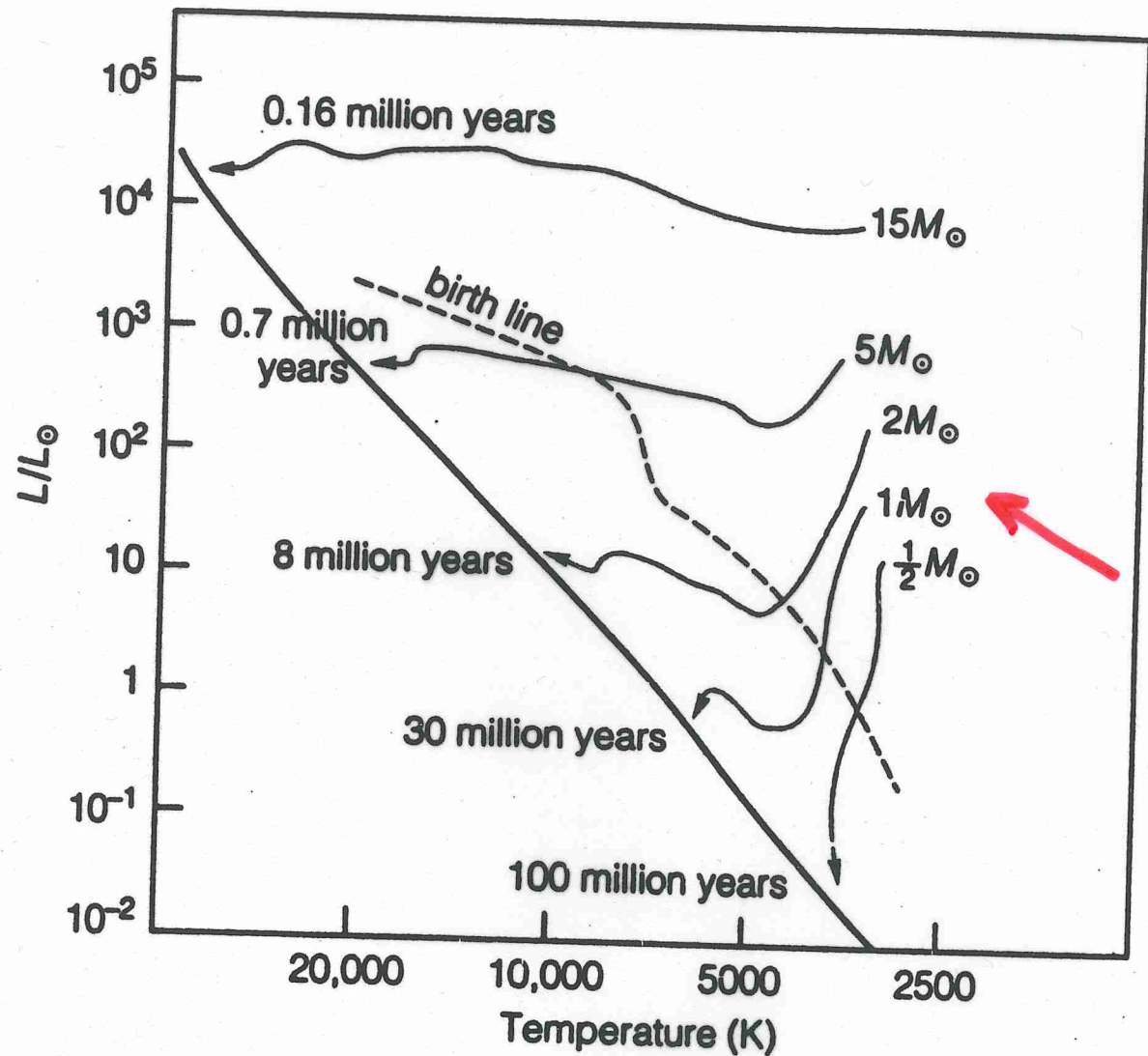
- GRAVITATIONAL ENERGY $\rightarrow$ HEAT
- SOME HEAT TRAPPED, SOME ESCAPES
- CENTRAL TEMPERATURE RISES
 $\rightarrow$ THERMAL PRESSURE RISE



• LATER COLLAPSE



- HAYASHI TRACK RAPID DROP IN L AT
~ CONSTANT T
- ENERGY REMOVED FROM CORE EFFICIENTLY
BY CONVECTION
- ENERGY USED TO BREAK UP H_2 MOLECULES
- CONVECTION CEASES AT BASE, STAR
BEGINS SLOW K-H CONTRACTION TO MAIN SEQ.



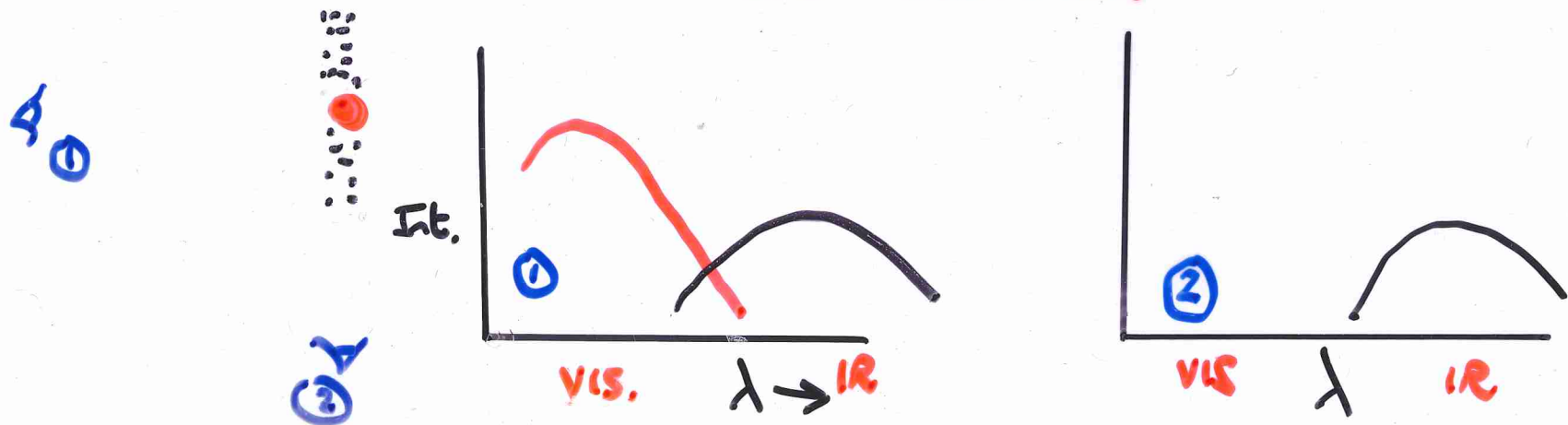
"KELVIN
- HELMHOLTZ"

FIGURE 12-5

The more massive a protostar is, the faster it contracts. A $1 M_{\odot}$ star requires 30 million years to reach the main sequence. The dashed line is the birth line, where contracting stars first become visible. (Illustration design by author)

PROTOSTARS ($\equiv$ pre-main sequence stars)

- SURROUNDED BY DUST, OFTEN IN A DISK
- DISK OF DUST MAY OBSCURE STAR
- PLANETS MAY FORM IN DISK
- DUST DISPERSED EVENTUALLY
- DUST REVEALED BY IR RADIATION



STELLAR EVOLUTION

INITIAL MASS

LESS THAN $8 M_{\text{SUN}}$

GREATER THAN
 $8 M_{\text{SUN}}$

REMNANT

WHITE DWARF

$$M_{\text{WD}} \leq 1.4 M_{\text{SUN}}$$

$\sim 0.6 M_{\text{SUN}}$ typically

NEUTRON STAR

$$M_{\text{NS}} \leq 3 M_{\text{SUN}}$$

OR

BLACK HOLE

$$M > M_{\text{NS}}, M_{\text{WD}} \\ \geq 3 M_{\text{SUN}}$$

WHAT'S THE NEXT STEP FOR He-RICH MAIN-SEQUENCE STARS?

- AS H SUPPLY IN CORE DECLINES, ENERGY SUPPLIED BY $4H \rightarrow He$ DECLINES TOO
- CORE MUST COLLAPSE: GRAVITY IN THE ASCENDANT
TEMPORARILY: H CONTINUES TO BURN IN SHELL AROUND CORE
- COLLAPSE $\rightarrow$ HEATING (KELVIN-HELMHOLTZ "We told you")
WITH TEMPERATURE RISING TO 200 MILLION KELVIN
- HOT CORE CAUSES OUTER LAYERS TO SWELL: STAR APPEARS AS RED GIANT/SUPERGIANT
- AT $T \sim 200$ MILLION K, HE BURNS: GRAVITY "FRUSTRATED" AGAIN.

He-BURNING



BUT ${}^8\text{Be}$ FLYS APART INTO 2 ${}^4\text{He}$ IN 10^{-16} seconds



${}^{12}\text{C}$ IS STABLE

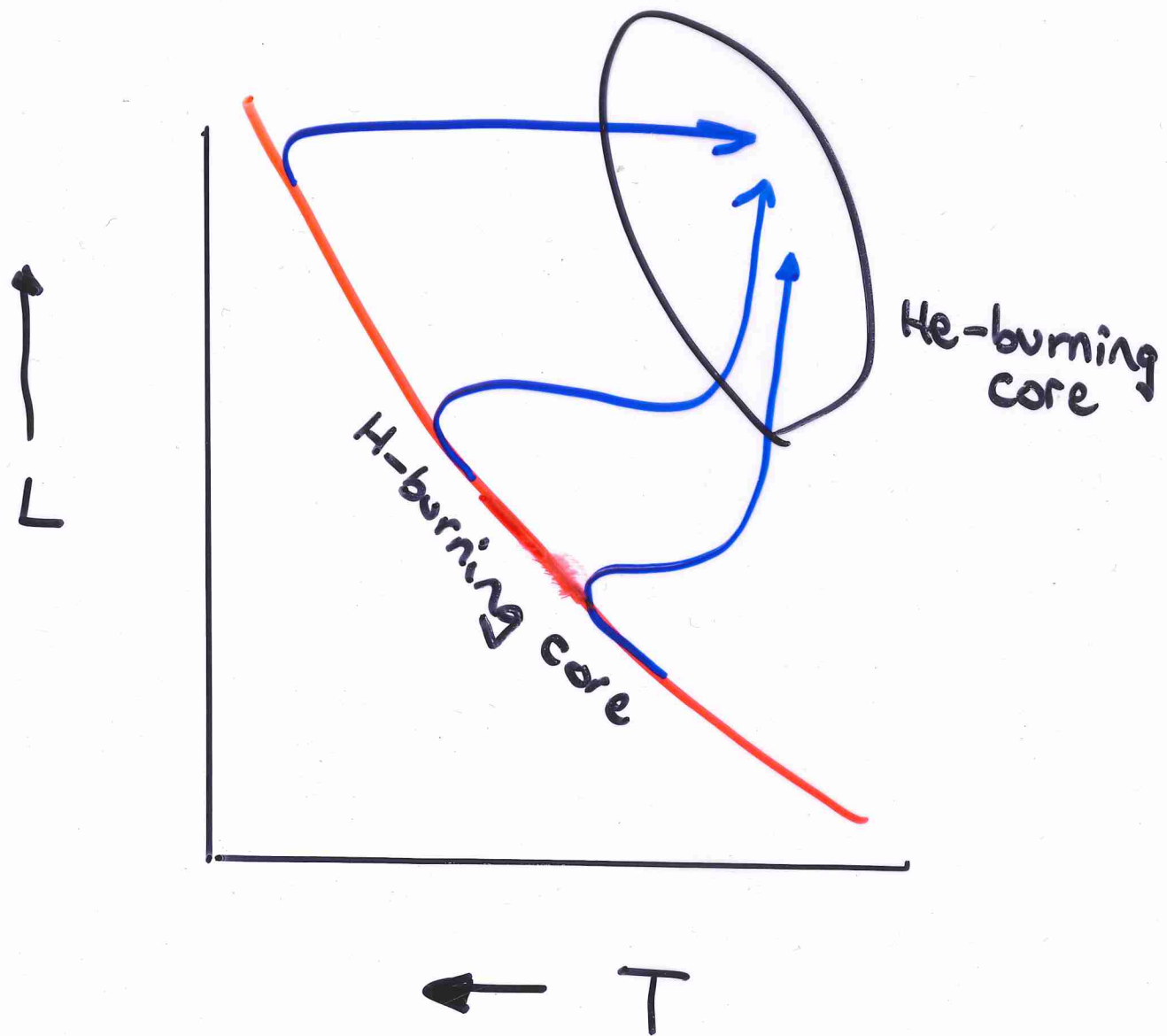
$\therefore$ THE PROCESS RUNS BY A TRIPLE COLLISION



"TRIPLE α PROCESS"

• AT HIGH TEMPERATURES, ALSO





- He-BURNING OCCURS AT
HIGHER TEMPERATURES
& HIGHER DENSITIES
THAN H-BURNING

- He-BURNING IS LESS EFFICIENT (10 TIMES)
THAN H-BURNING

SUN : $\begin{cases} 10^{10} \text{ years for H-burning} \\ 200 \times 10^6 \text{ years for He-burning} \end{cases}$

- ALL STARS EXPERIENCE He-BURNING
- $\begin{cases} \text{HIGH MASS STARS BURN C AND O} \\ \text{LOW MASS STARS DO NOT} \end{cases}$