

New Cosmological Hydrodynamic Code Developments

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Motivations – GCs as fossil records of galaxies

Globular star clusters (GCs)

- the oldest bound stellar system in the universe
- typical mass and size : $\sim 10^5 M_{\odot}$ ($\sim M_V = -5$ to -10), a few parsecs
- The characteristics of GC systems are correlated with properties of their parent galaxies.
 - : metal bimodality, specific frequency, size dist., radial dist., and so on

Motivations - GCs & Reionization

The previous studies on GCs & reionization

1. GC formation was suppressed by the reionization

- Beasley et al. 2002, Santos 2003, Bekki 2005, Moore et al. 2006, Spitler et al. 2012

2. GCs reionized the universe

- Ricotti 2002, Power et al. 2009, Schaerer & Charbonnel 2011, Griffen et al. 2012

3. GC formation was triggered by the reionization

- Cen 2001, Hasegawa et al. 2009

4. GC formation rate using UV luminosity function

- Katz & Ricotti 2012

Motivations

GCs to constrain the below

- the star formation and assembly histories of galaxies
- the nucleosynthetic processes governing chemical evolution
- the epoch and homogeneity of cosmic reionization
- the role of dark matter in the formation of structure in the early universe
- the distribution of dark matter in present-day galaxies

Strategies

To simulate the sub-galactic scale structure formation in the Lambda CDM model,
we have developed [a new cosmological hydrodynamic code](#).

- using the most efficient code (PM+tree) for the large scale structure, [GOTPM](#) (Dubinsky, Kim, & Park 2003),
- improved [the hydrodynamics](#) (SPH) into the GOTPM code (mainly by Juhan Kim)
- added the [realistic baryonic physics](#) (in preparation, Shin, Kim, & Kim 2013)
 - : Reionization process by UV background sources and UV shielding
 - : Radiative heating/cooling ($T \sim$ reach to 100K)
 - : Star formation as single stellar population
 - : Metal, mass and energy feedback by SN_{II}

Targeted mass resolution is $\sim 10^3 M_{\text{sun}}$

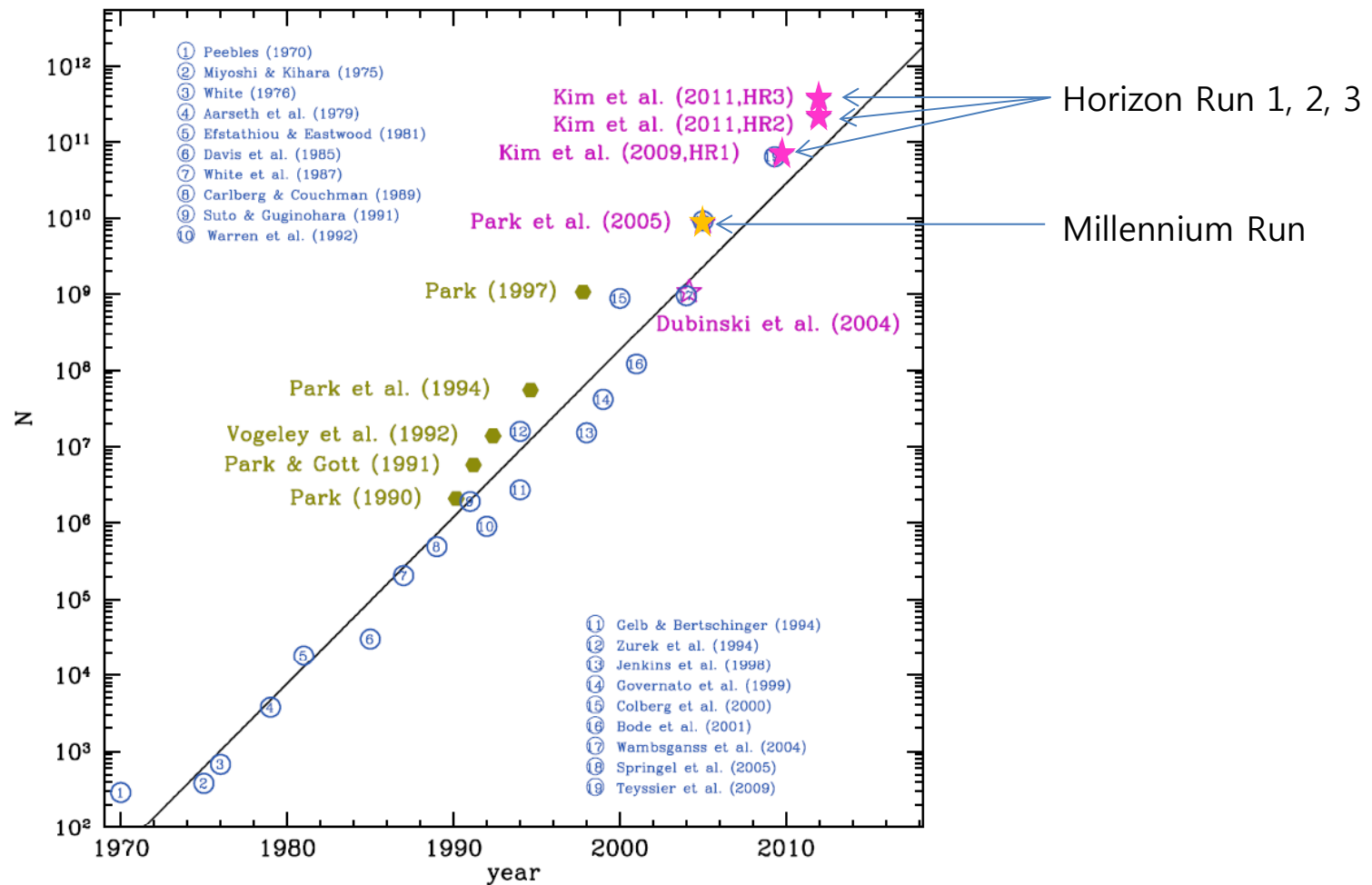
- : from [globular clusters](#) to galaxy groups (box size up to $\sim 32 \text{ Mpc}/h$)
- : using zoom-in technique and powerful computer resources

GOTPM (Dubinski, Kim, Park, & Humble 2003)

- based on a hybrid scheme using the [particle-mesh \(PM\)](#) and [Barnes-Hut \(BH\) oct-tree algorithm](#)
- used for recent large-volume simulations : Horizon Run 1, 2, 3 (7210^3 particles, 10.815 Gpc/h side length)

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SPH (Smoothed-Particle Hydrodynamics)

- A version of the Lagrangian scheme in the hydrodynamics
- Following the entropy-conservation method (Springel & Hernquist 2003)
- Efficient memory consumption : 104 byte/particle (152byte/particle, GADGET-2)
- Individual time-step based on the Kick-Drift-Kick scheme (Springel 2005)
- Glacial initial condition : random positioning of the baryonic matter $N_{baryon} = N_{total} \times (\Omega_{baryon}/\Omega_{matter})$

$$\rho_i = \sum_{j=1}^{N_{nbg}} m_j W(\vec{r}_i - \vec{r}_j, h_i), \quad P_i = A_i \rho_i^\gamma = (\gamma - 1) \rho_i u_i,$$

$$\frac{d\vec{v}}{dt} = - \sum_{l=1}^{N_{nbg}} m_j \left[f_l \frac{P_l}{\rho_l^2} \nabla_l W_{lj}(h_l) + f_j \frac{P_j}{\rho_j^2} \nabla_j W_{lj}(h_j) + m_j \Pi_{lj} \nabla_l W_{lj} \right],$$

$$\frac{du_i}{dt} = f_i \frac{P_i}{\rho_i} \sum_{j=1}^{N_{nbg}} m_j (\vec{v}_i - \vec{v}_j) \cdot \nabla W_{ij}(h_i) + \frac{1}{2} \sum_{j=1}^{N_{nbg}} m_j \Pi_{ij} \vec{v}_{ij} \cdot \nabla W_{ij}(h_i),$$

$$\Pi_{ij} = - \frac{\alpha (c_i + c_j - 3\omega_{ij}) \omega_{ij}}{2 \rho_{ij}},$$

$$\Delta t^{SPH} = \frac{C_{courant} h_i}{\max_j (c_i + c_j - 3\omega_{ij})}.$$

Cooling/Heating

Including non-adiabatic process on the evolution of the baryons

Using the publicly available photoionization package **CLOUDY 90** (Ferland et al. 1998)

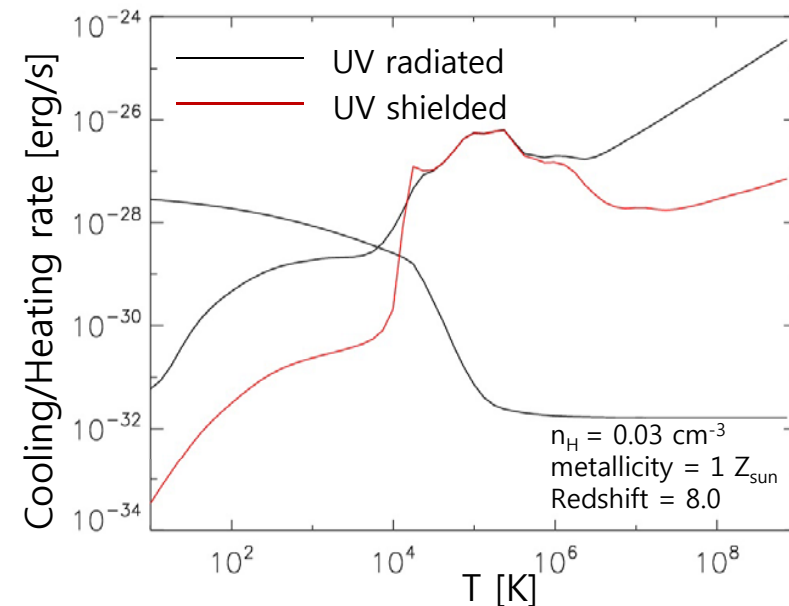
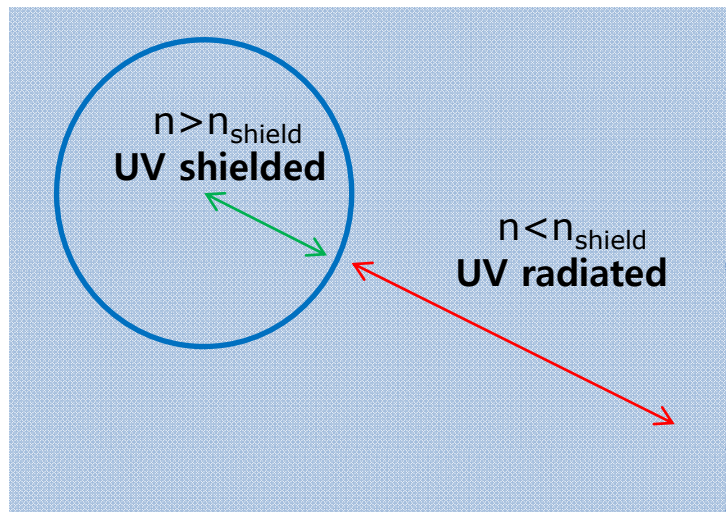
- functions of density, temperature, metallicity and redshift

Tabulating the cooling/heating rates as **existence of the uniform UV/X-ray background** (Haardt & Madau 2001)

- Average thermal evolution before and after the reionization ($z=8.9$)
 - : collisional ionization for $z>8.9$ and photoionization for $z<8.9$
- **self-shielding from the UV background radiation** ($n_{\text{shield}} = 0.014 \text{ cm}^{-3}$ following Tajiri & Umemura 1998)

$n_{\text{H}} < n_{\text{shield}}$: UV radiated medium

$n_{\text{H}} > n_{\text{shield}}$: UV shielded medium



Star Formation

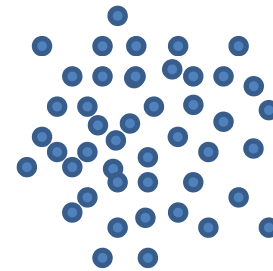
Converting gas particles into star particles

Star formation criteria :

(Katz et al. 1996)

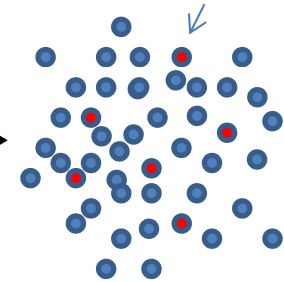
$$\begin{aligned} T &< 10^4 \text{ K} \\ n_{\text{H}} &> 0.1 \text{ cm}^{-3} \\ \nabla \cdot \mathbf{v} &< 0 \\ \rho &> 57.7 \rho_{\text{g}}(z) \end{aligned}$$

SF eligible particles



Δt

star particle

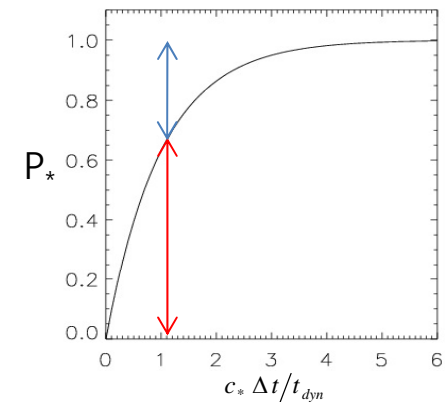


Star formation rate (c_*) : calibrated by the Schmidt-Kennicutt relation

$$\frac{d\rho_*}{dt} = c_* \frac{\rho_{\text{gas}}}{t_{\text{dyn}}} \quad (\text{global star-formation properties, Kennicutt 1998})$$

$$\text{Star formation probability : } p_* = \frac{m_{\text{gas}}}{m_*} \left[1 - \exp\left(-c_* \frac{\Delta t}{t_{\text{dyn}}}\right) \right]$$

$$m_{\text{gas}} / m_* = 3, \quad c_* = 0.033$$



Containing a single stellar population

: Location, velocity, mass, metallicity - inherited from the parent gas particles

: **Stellar mass function** - Kroupa (2001) with range of $0.1 M_{\text{sun}} \sim 100 M_{\text{sun}}$

Feedback (SN_{II})

- Implementing feedback in a probabilistic manner

(Okamoto, Nemmen, and Bower 2008)

$$P_{SN} = \frac{\int_{t_{SSP,i}}^{t_{SSP,i}+dt} r_{SNII}(t') dt'}{\int_{t_{SSP,i}}^{t_8} r_{SNII}(t') dt'}$$

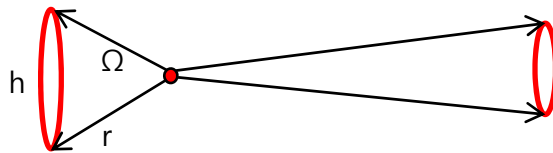
- Distributing feedback to neighbor gas particles

1. energy feedback

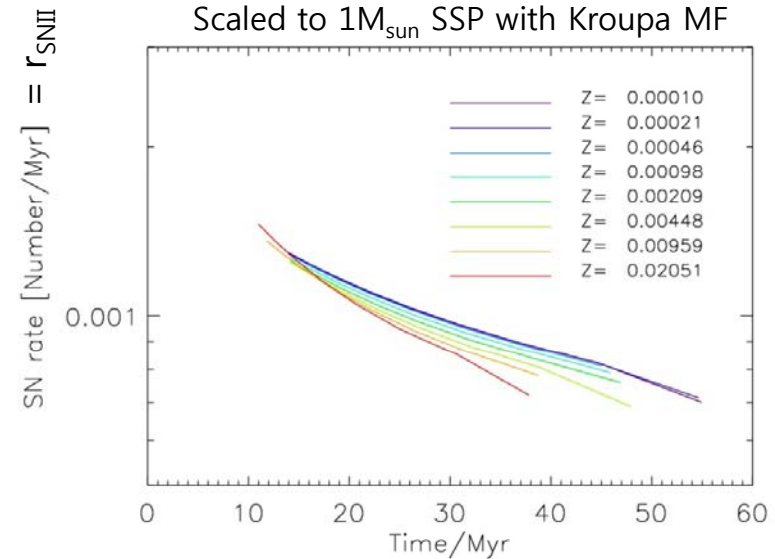
- ΔE of star particle : $\sim 10^{51} \text{erg}/1 \text{ SN}_{II}$
- **overcooling problem : a new scheme of the individual time-step limiter** (Saitoh & Makino 2009)
- leading to a self-regulated cycle for star formation activity

2. metal and mass feedbacks

- released metal : $\Delta Z = \int \Psi(m) m_{ej,metal}(m, Z) dm / \Delta M_{SN}$, $m_{ej,metal}(m, Z)$ from Woosley & Weaver (1995)
- proportional to solid angles of neighbors :



- metallicity-dependent heating/cooling



$$\Omega_i \propto h_i^2 / r_i^2 \propto n_i^{-2/3} / r_i^2$$

$$\Delta Z_{SN,i} = m_i n_i^{-2/3} r_i^{-2} \Delta Z_{SN} / \sum_{j=1}^N m_j n_j^{-2/3} r_j^{-2}$$

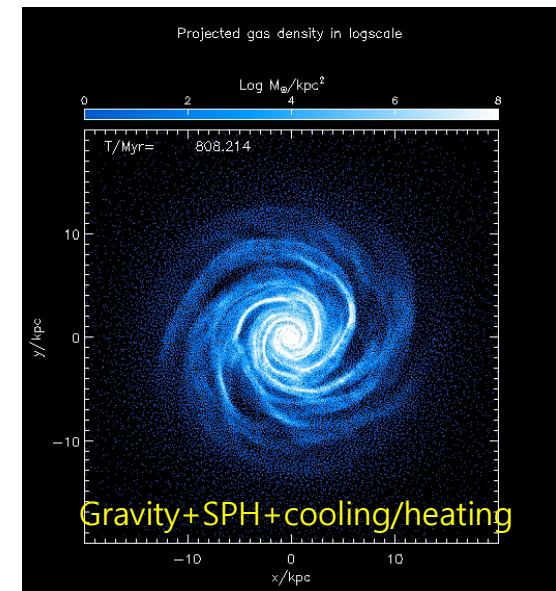
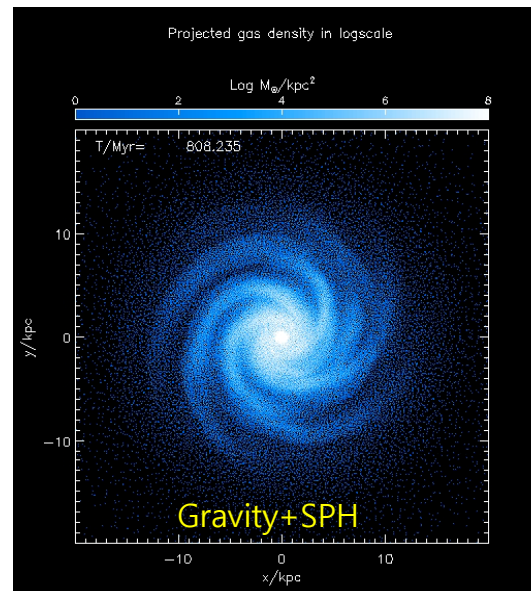
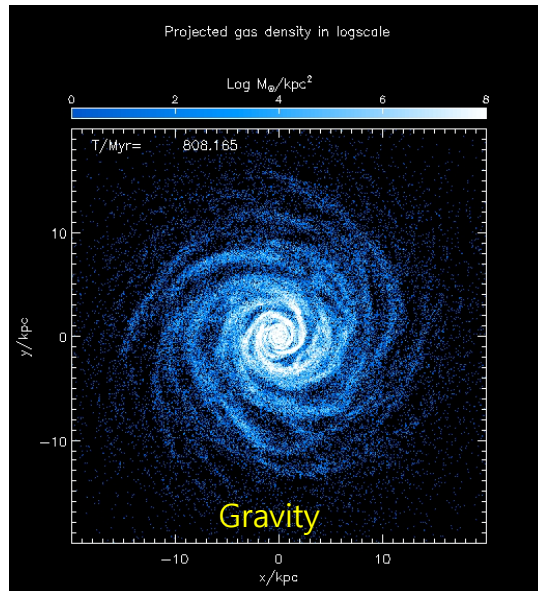
Test Run in Non-Cosmological Frame

Evolution of an isolated galaxy

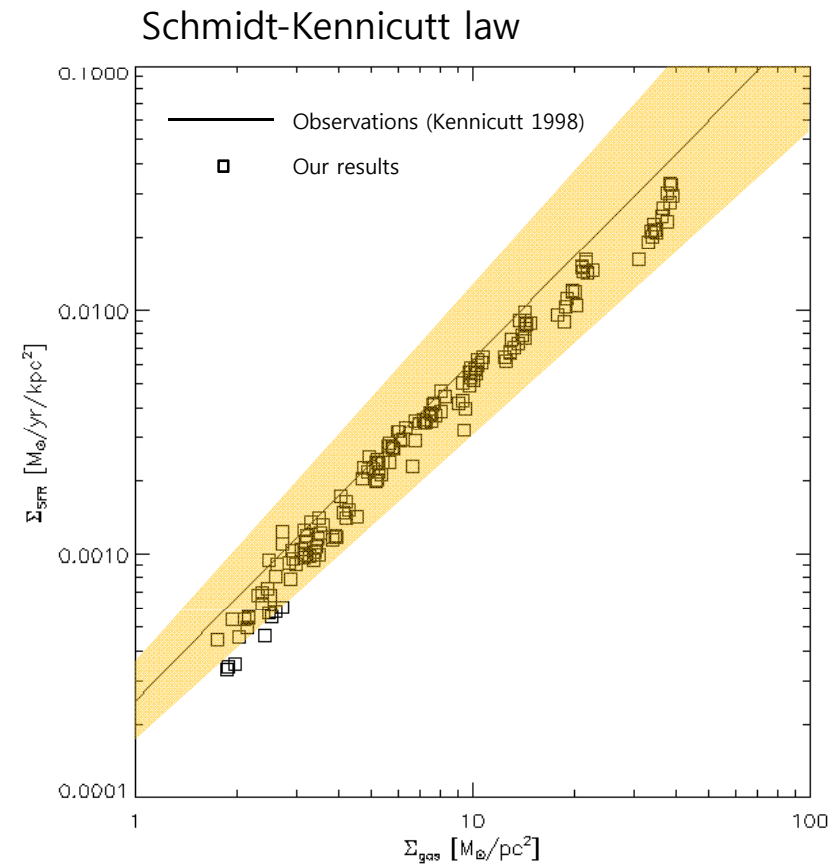
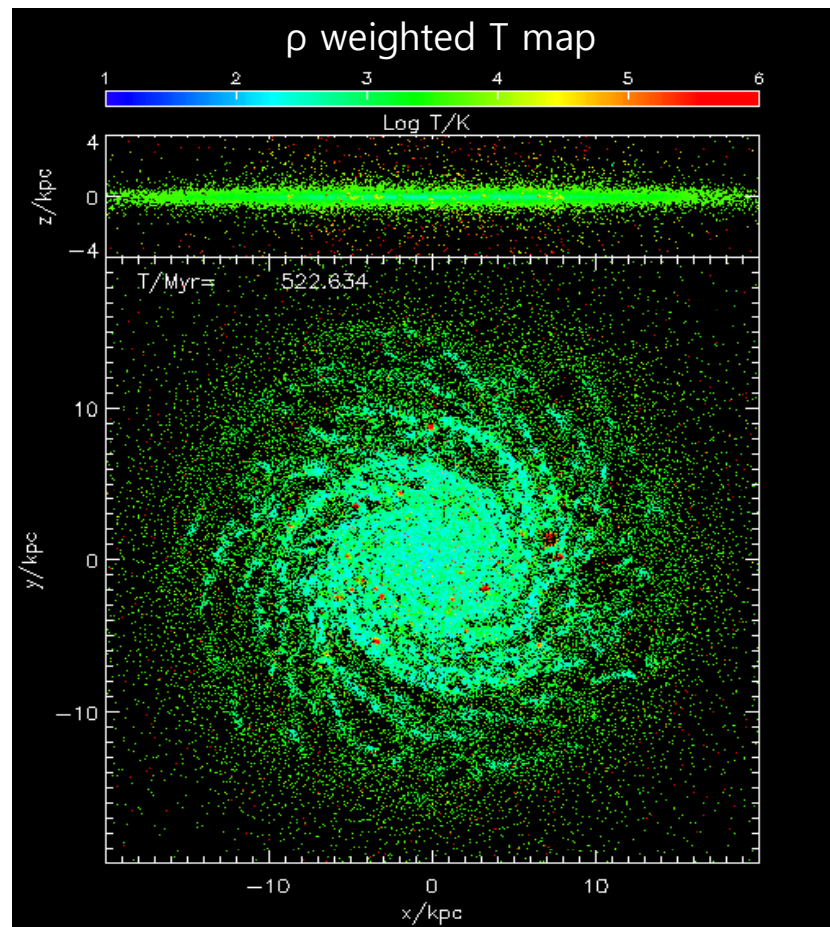
- to check how well the new implementation reproduce the Schmidt-Kennicutt law
- modified the GOTPM code to handle the non-expanding coordinate (scale length = constant)
- using a compound galaxy model as the initial condition for the test

	Particle number	Particle mass	Potential model	Parameter
Gas disk	98304	$4.196 \times 10^4 M_{\text{sun}}$	Exponential Disk	$M = 4.125 \times 10^9 M_{\text{sun}}$, $z = 0.3 \text{ kpc}$, $h = 3.33 \text{ kpc}$
Stellar disk	884736	$4.196 \times 10^4 M_{\text{sun}}$	Exponential Disk	$M = 3.715 \times 10^{10} M_{\text{sun}}$, $z = 0.3 \text{ kpc}$, $h = 3.33 \text{ kpc}$
Bulge	Fixed	-	Hernquist profile	$M = 1.375 \times 10^{10} M_{\text{sun}}$, $a = 0.8 \text{ kpc}$
Halo	Fixed	-	Hernquist profile	$M = 2.2 \times 10^{11} M_{\text{sun}}$, $a = 10 \text{ kpc}$

Initial conditions from ZENO by Barnes

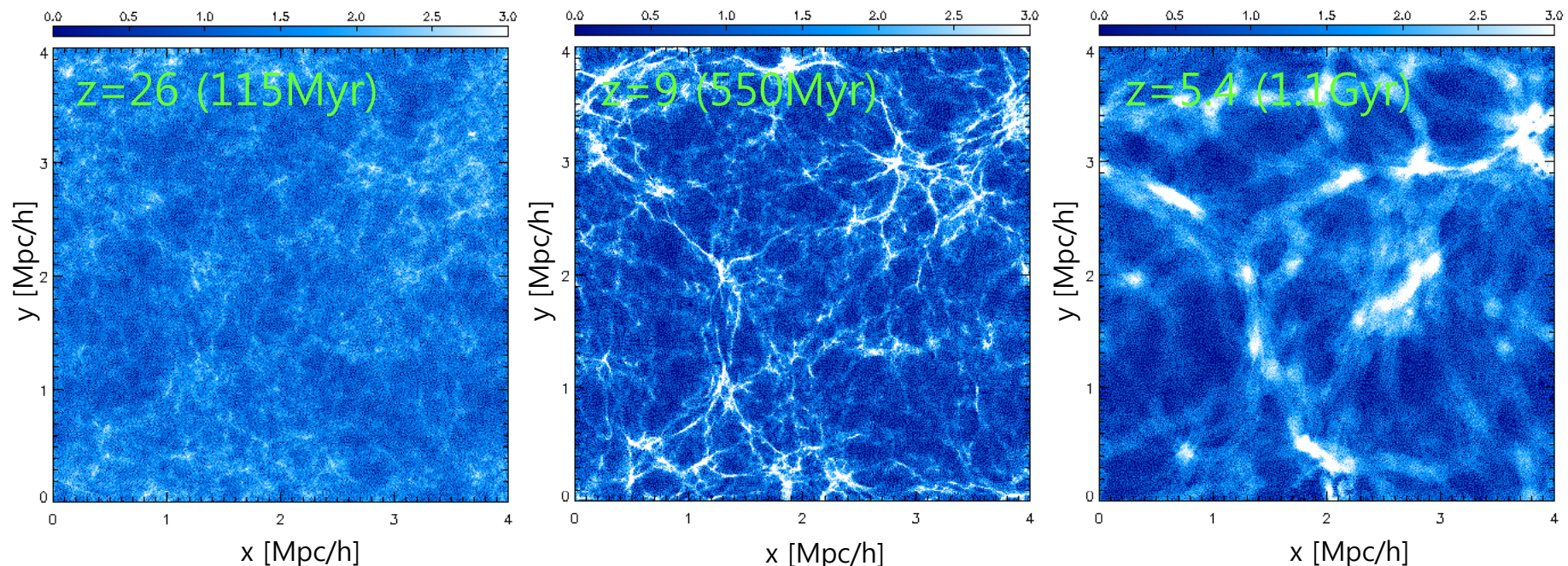


Gravity + SPH + Cooling/Heating + SF + SN feedback



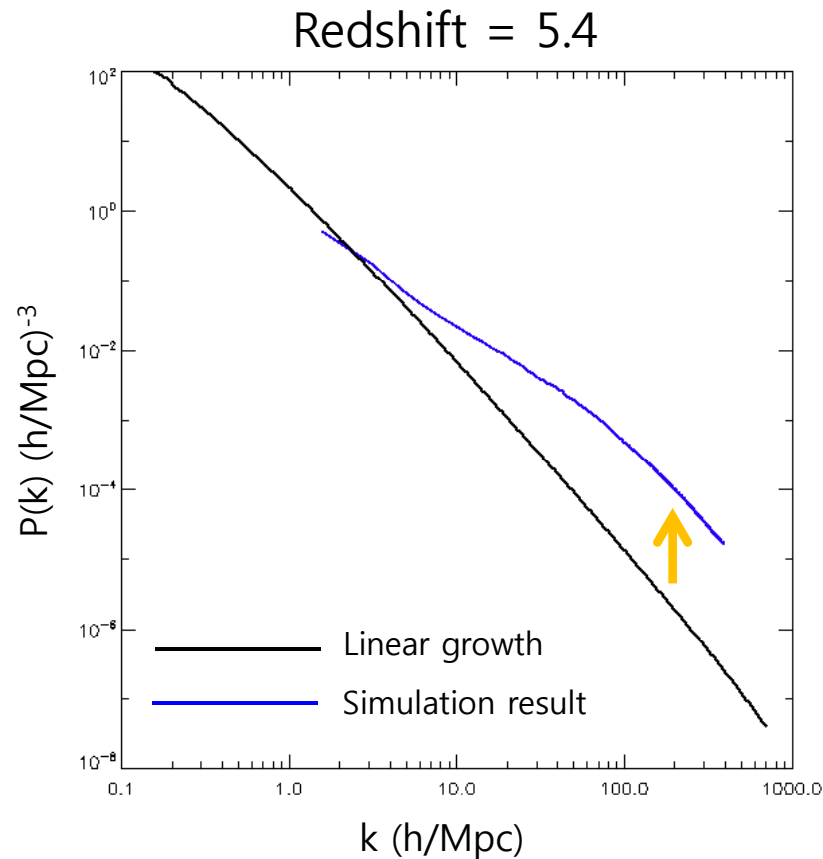
Test Runs in the Cosmological Frame

- We have performed a cosmological hydrodynamic simulation with the new code.
 - a cubic box with a side length of 4 Mpc/h with 512^3 (130 million) particles
 - mass resolution $\sim 3.4 \times 10^4 M_\odot$ (sub-galactic halos are resolved with more than hundred particles)
 - initial condition : $p(k)$ at $z = 150$ (CAMB package) and initial displacement (Zel'dovich's approximation)
 - Λ CDM cosmology : WMAP-5th yr parameter ($\Omega_m=0.26$, $\Omega_\Lambda=0.74$, $\Omega_b=0.044$, $\sigma_8=0.76$, $h=0.72$)
 - used 64 cores for one month down to $z=5.4$

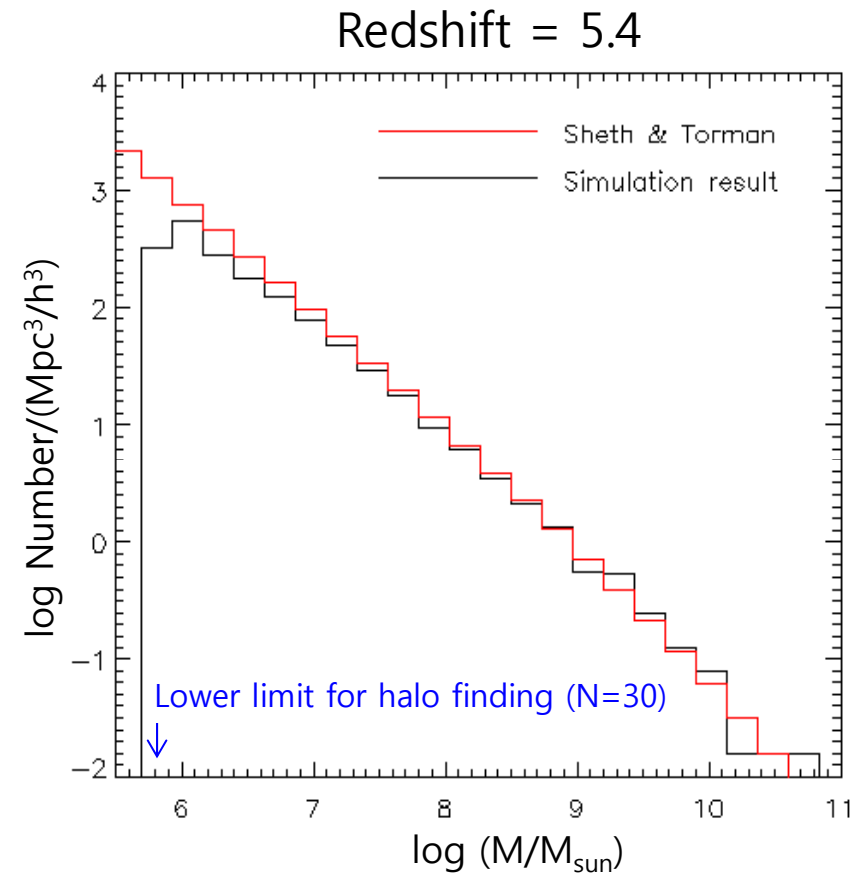


Projected gas density in logscale [$\text{Log } M_\odot/\text{kpc}^2$] at three different epochs

Comparison with theoretical predictions



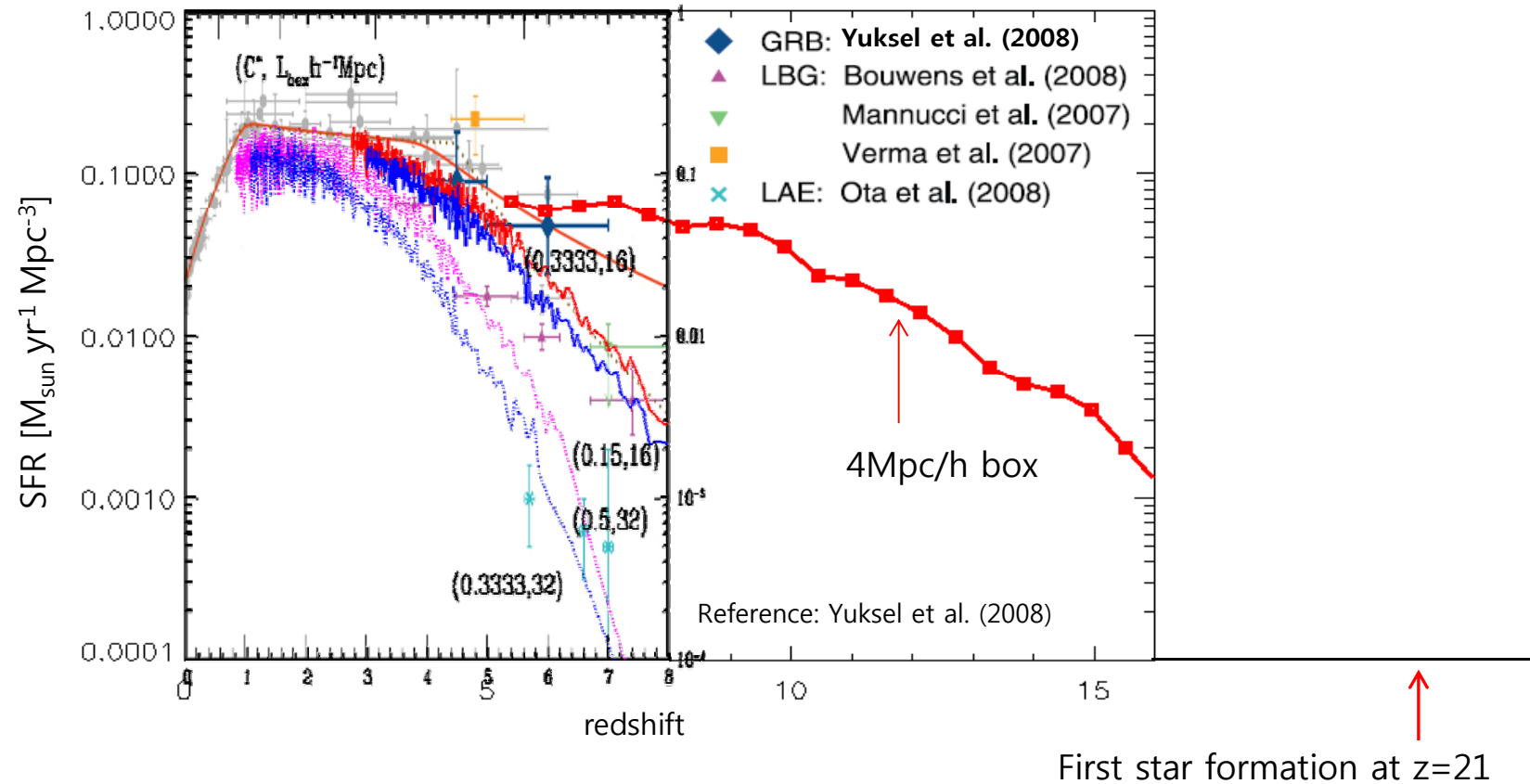
Power spectrum of cold dark matters



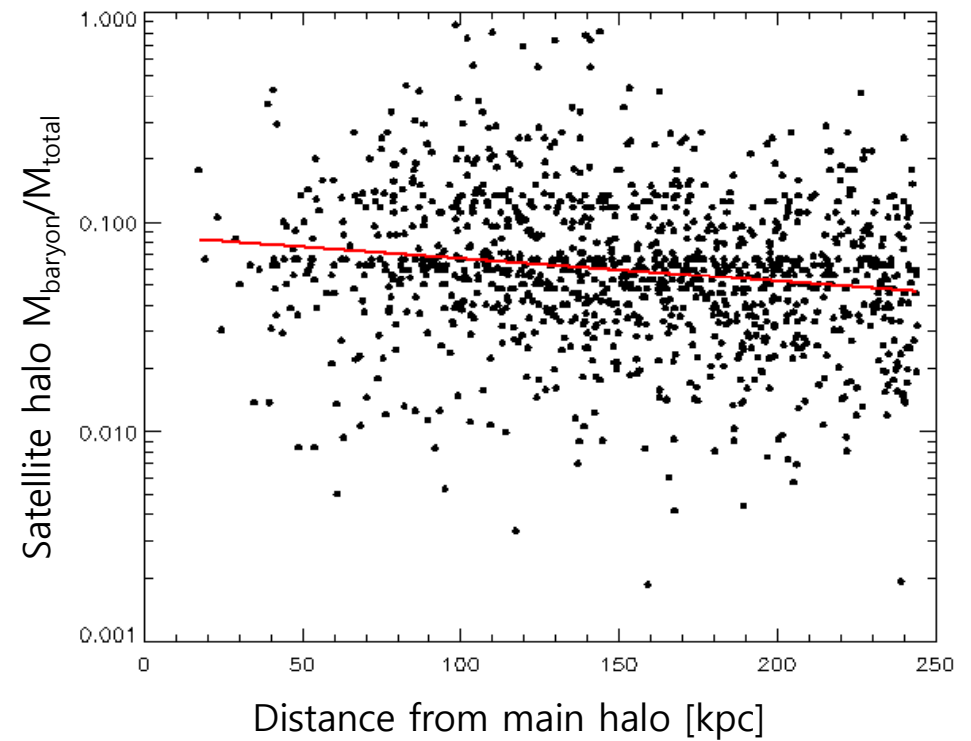
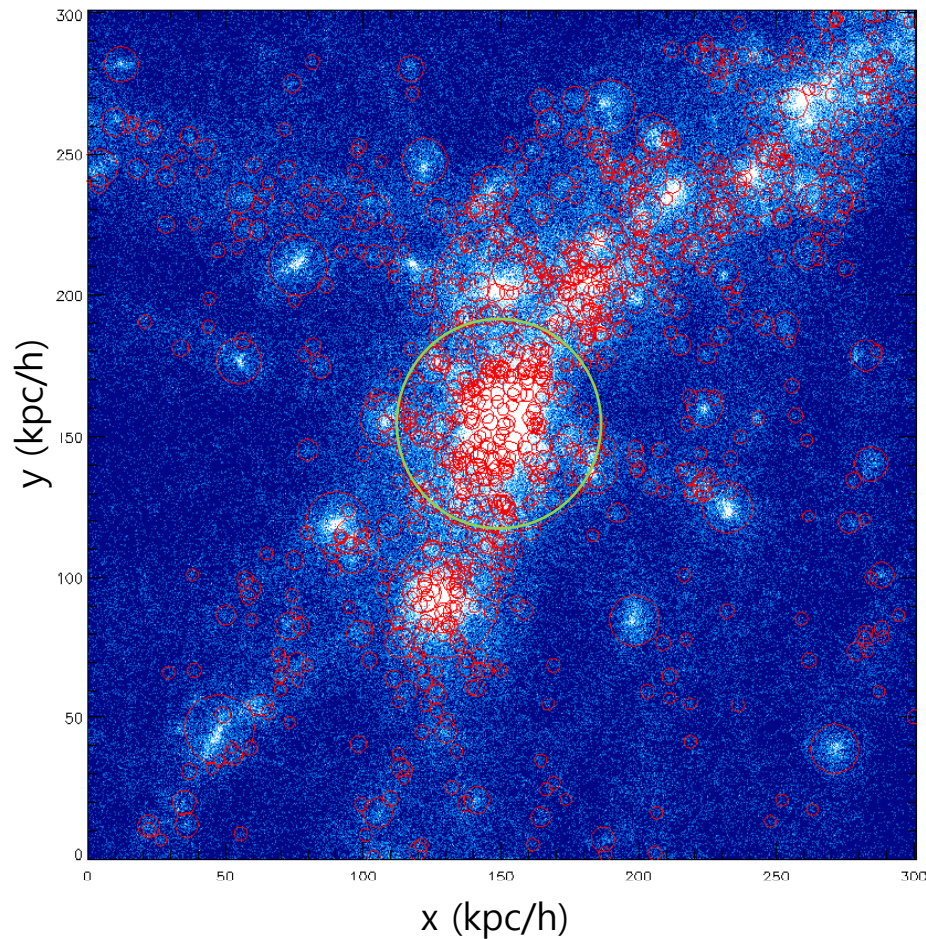
Dark matter mass function

Halo finding : Friend-of-Friend (FoF) & hierarchical FoF

Comparison with observations



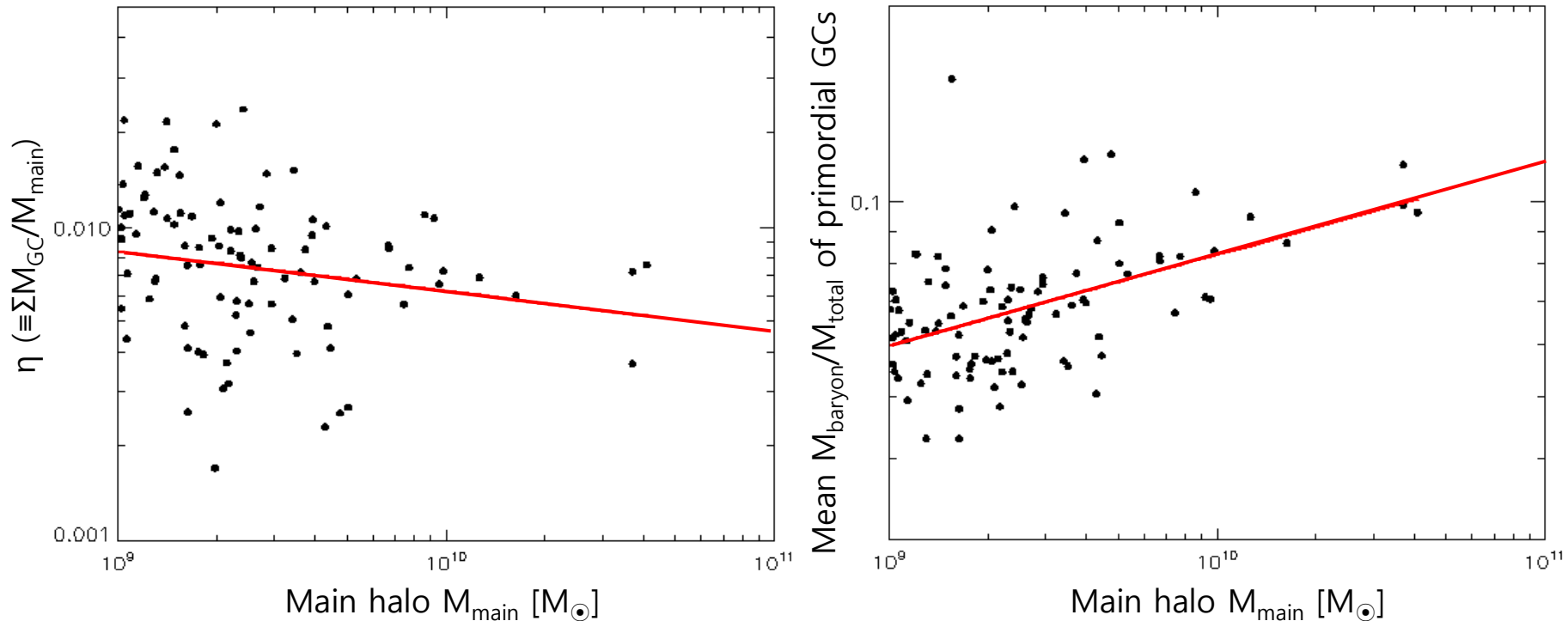
Distribution of satellite halos around a $\sim 10^{10} M_{\odot}$ main halo at $z = 5.4$



$M_{\text{baryon}}/M_{\text{total}}$ of satellite haloes vs.
their distances from the main halo

Properties of Globular Cluster Candidates

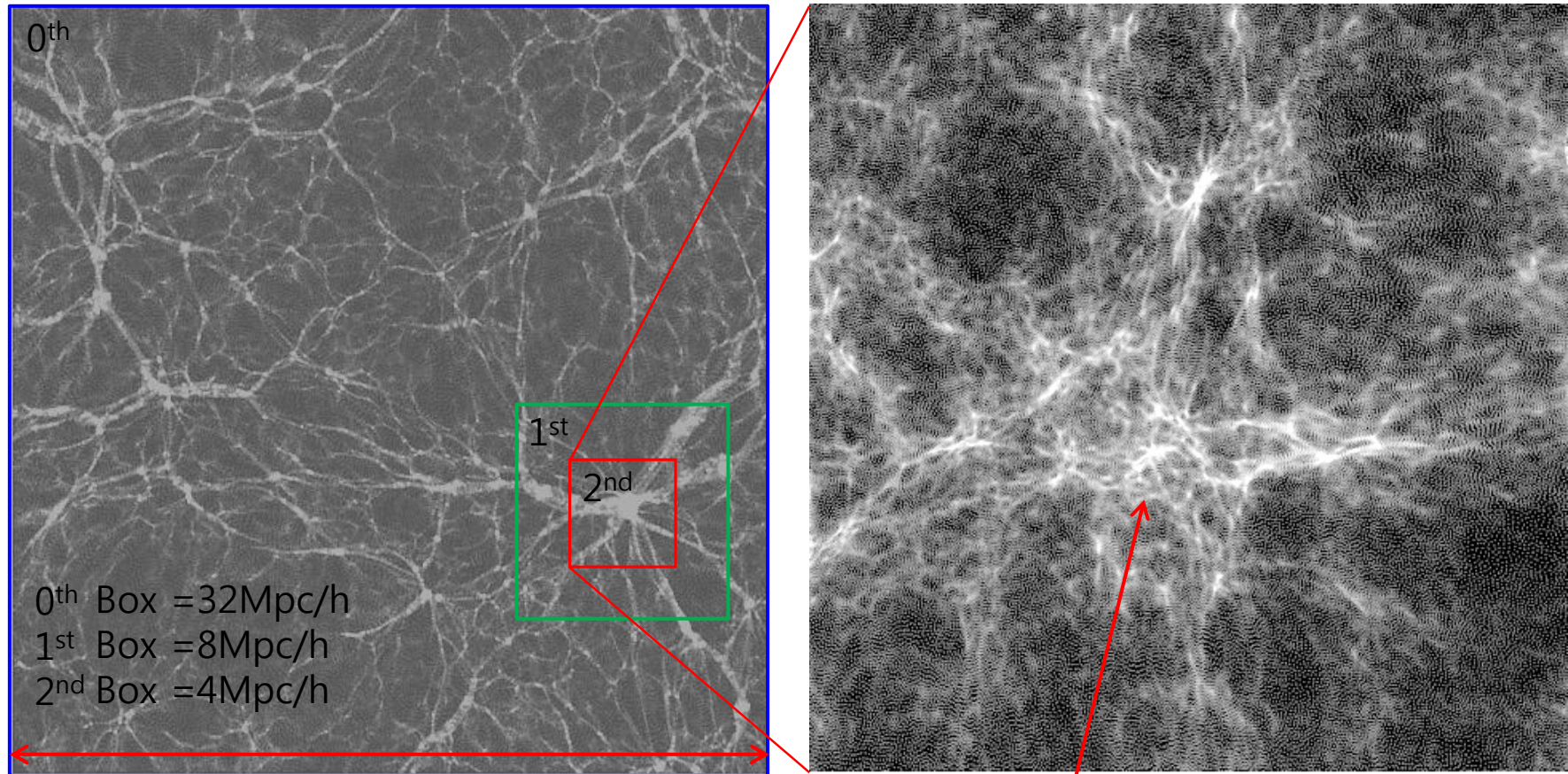
Specific mass and mean $M_{\text{baryon}}/M_{\text{total}}$ of GC candidates at $z=5.4$



- η ($\equiv \Sigma M_{\text{GC}}/M_{\text{main}}$: Specific GC formation efficiency) of the main halos at $z=5.4$ is ~ 2 orders of magnitude larger than the previous estimates of $\sim 10^{-4}$ – 10^{-5} (Blakeslee 1999; Kravtsov & Gnedin 2005; Spitler & Forbes 2009).
- A large fraction of GCs around the main halo at $z=5.4$ will be disrupted during the continuous accretion into the main halo and constitute the main halo.

Zoom-in Simulation

We just finished applying **zoom-in technique** into the our new GOTPM+SPH code



GCs & Reionization

The previous studies on GCs & reionization

1. GC formation was suppressed by the reionization

- Beasley et al. 2002, Santos 2003, Bekki 2005, Moore et al. 2006, Spitler et al. 2012

2. GCs reionized the universe

- Ricotti 2002, Power et al. 2009, Schaerer & Charbonnel 2011, [Griffen et al. 2012](#)
= Aquarius DM halo + C²-Ray

3. GC formation was triggered by the reionization

- Cen 2001, Hasegawa et al. 2009

4. GC formation rate using UV luminosity function

- Katz & Ricotti 2012

To do : ray tracing method + our code

Future work

1. Complete the code developments
 - zoom-in technique, especially the boundary particles
 - multi-phase model, H₂ cooling, and H₂ dependent star formation
 - stability and performance tests
 - using GPU
2. Perform the high resolution simulation
 - formation of GCs around the Milky-Way like galaxy
 - relations between properties of GCs and that of the host galaxies
 - GCs as tracers for the history of galaxies
3. Correlation between GCs and the cosmic reionization
 - implementing ray-tracing
 - origin of the bimodal distribution of globular clusters

Thank you very much