

# SimpleX

## Radiative Transfer on an Unstructured Dynamic Grid

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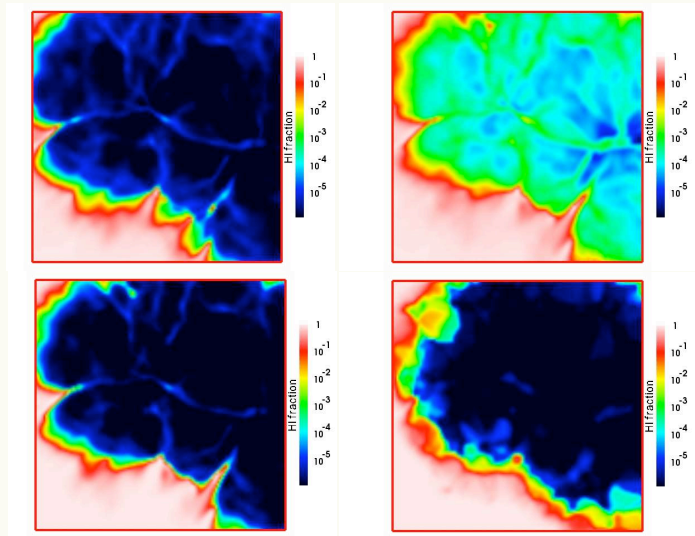
## Comparison Paper 1

SimpleX participated in first comparison paper

New features:

Parallel

Better performance in optically thin regimes



Iliev et al. 2006

Introduction

SimpleX

Test 1

Test 4

Conclusions

## Structured Grids

### Nature is not cubical!

#### A regular mesh introduces errors

Physical symmetries are broken

- Rotational
- Translational

Unphysical conserved quantities

Superimposed scale lengths

Introduction

SimpleX

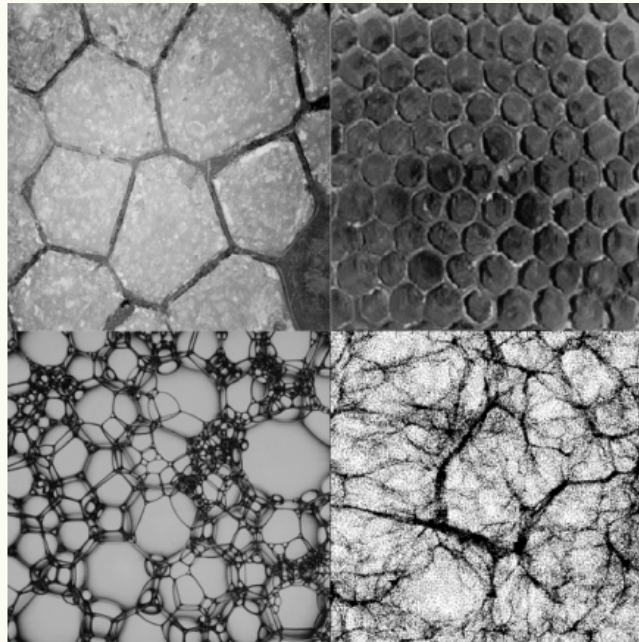
Test 1

Test 4

Conclusions

Unstructured  
Grid

## Nature resembles Voronoi diagram!



Ritzerveld 2007

Reconstructed (density) fields are optimal in the sense of defining a continuous and unbiased representation of the data while retaining all information available in the point sample (Schaap, 2006)

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Conclusions

Voronoi  
Delaunay  
Grid

Voronoi - Delaunay grid resembling underlying physics

Probabilistic treatment of radiative transfer

Migration of photons is Markov stochastic process

Microscopic statistics → Macroscopic quantities

Introduction

**SimpleX**

Test 1

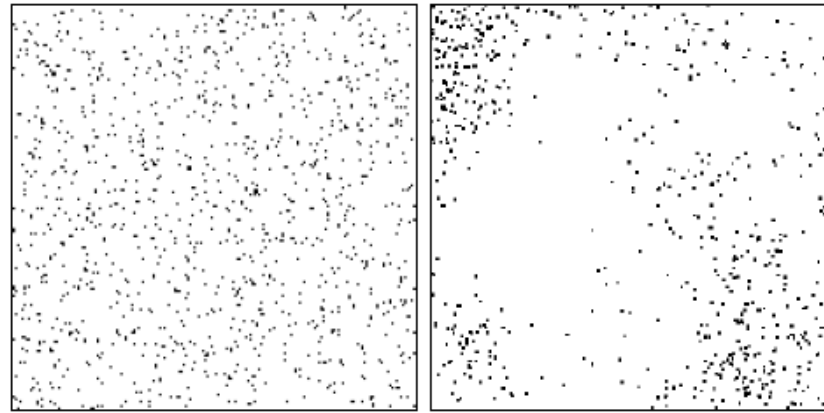
Test 4

Conclusions

Unstructured  
Grid

Stochastic point process determines placement of grid points

Higher opacity → More points



Homogeneous  
Poisson process

Clumpy  
Correlated process



Introduction

**SimpleX**

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Conclusions

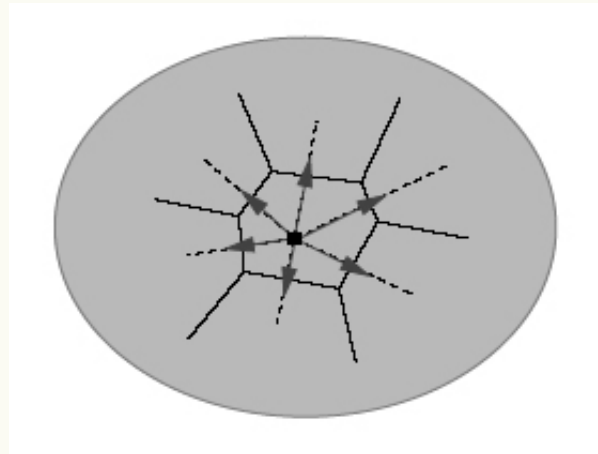
## Voronoi Delaunay Grid

Voronoi Tessellation:

$$C_i = \{y \in \mathbb{R}^d : \|x_i - y\| \leq \|x_j - y\| \forall x_i \neq x_j\}$$

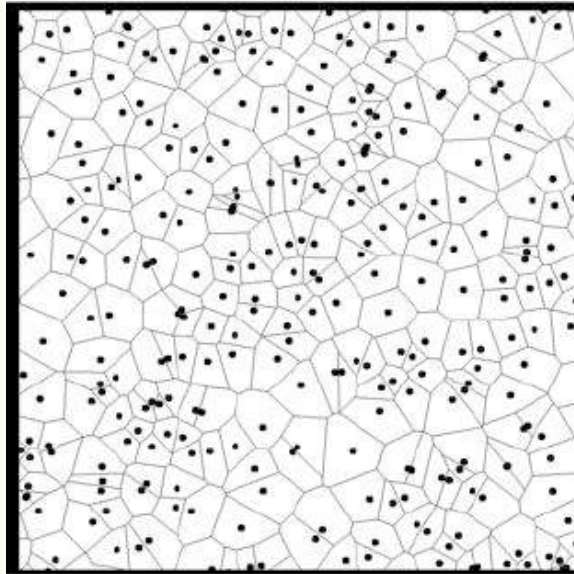
Delaunay Triangulation:

Connect all nuclei whose cells have a common facet

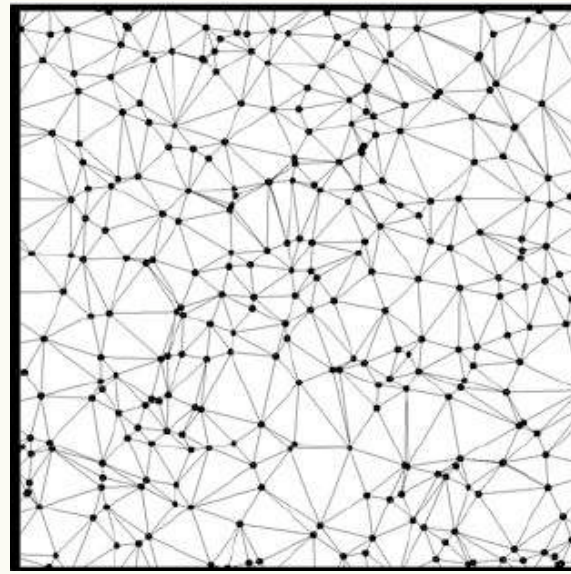


Voronoi  
Delaunay  
Grid

Homogeneous example



Voronoi Tessellation



Delaunay Triangulation

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Voronoi  
Delaunay  
Grid

Properties of the Delaunay grid

Local mean free path:

$$\lambda(\vec{x}) = \frac{1}{n(\vec{x})\sigma}$$

$n(\vec{x})$  density distribution

Average Delaunay line length:

$$\lambda_D(\vec{x}) = \frac{\zeta}{n_D(\vec{x})^{\frac{1}{d}}}$$

$n_D(\vec{x})$  local point distribution

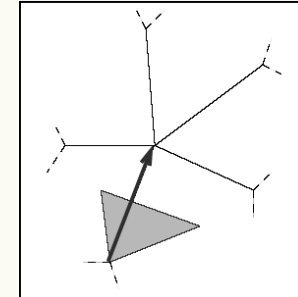
Choose point distribution sampling  $n(\vec{x})^d$ :

$$\lambda_D(\vec{x}) = c \lambda(\vec{x})$$

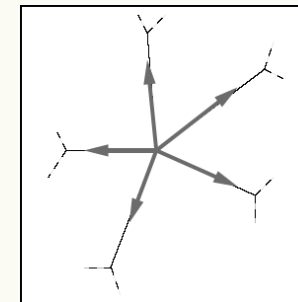
➔ Mean free path is constant on grid!

# Photon Transport

Photons are transported along Delaunay lines



A source sends photons to every neighbour



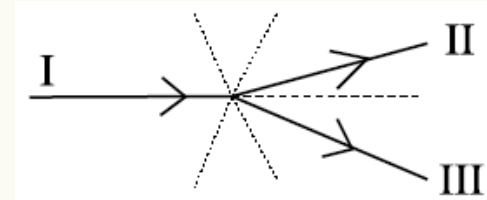
Travel distance of photons correlates linearly with the optical depth

$$c = \xi(d, N, D) \sigma$$

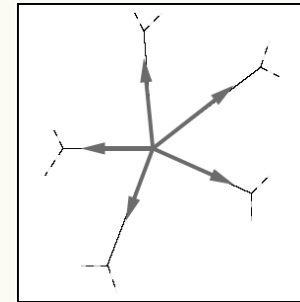
$\xi(d, N, D)$  constant  
 $\sigma$  cross section

Photon Transport

Outgoing intensity is  $I_{out} = I_{in}e^{-c}$



Retained intensity is  $I_{ret} = I_{in}(1 - e^{-c})$

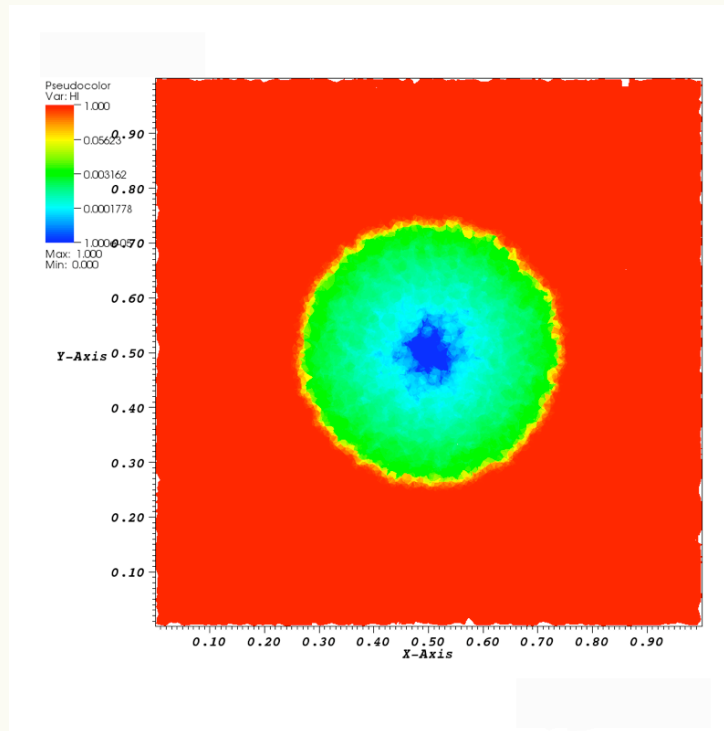


SimpleX does NOT scale with the number of sources!

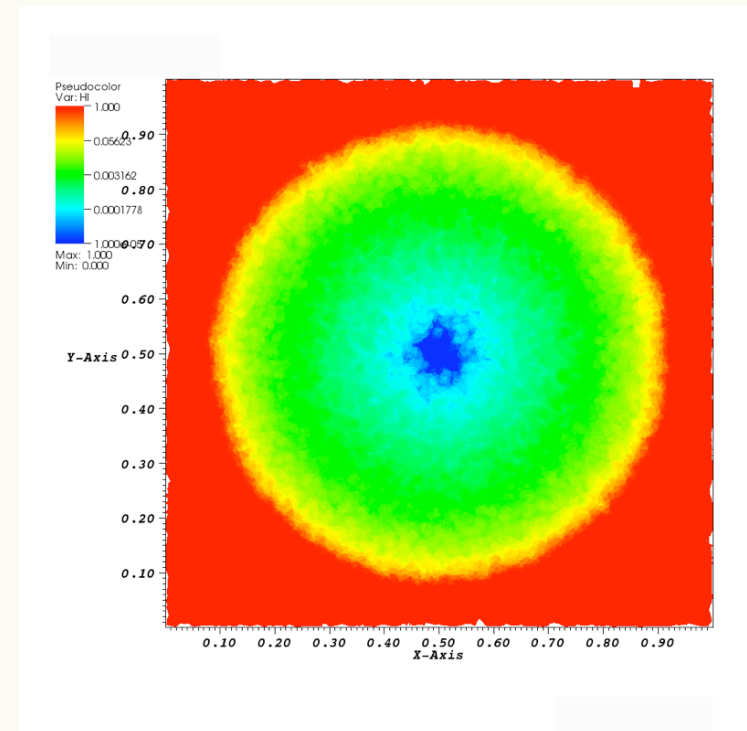
Results  
Test 1

HII region expansion in homogeneous medium (Test 1)

30 Myr

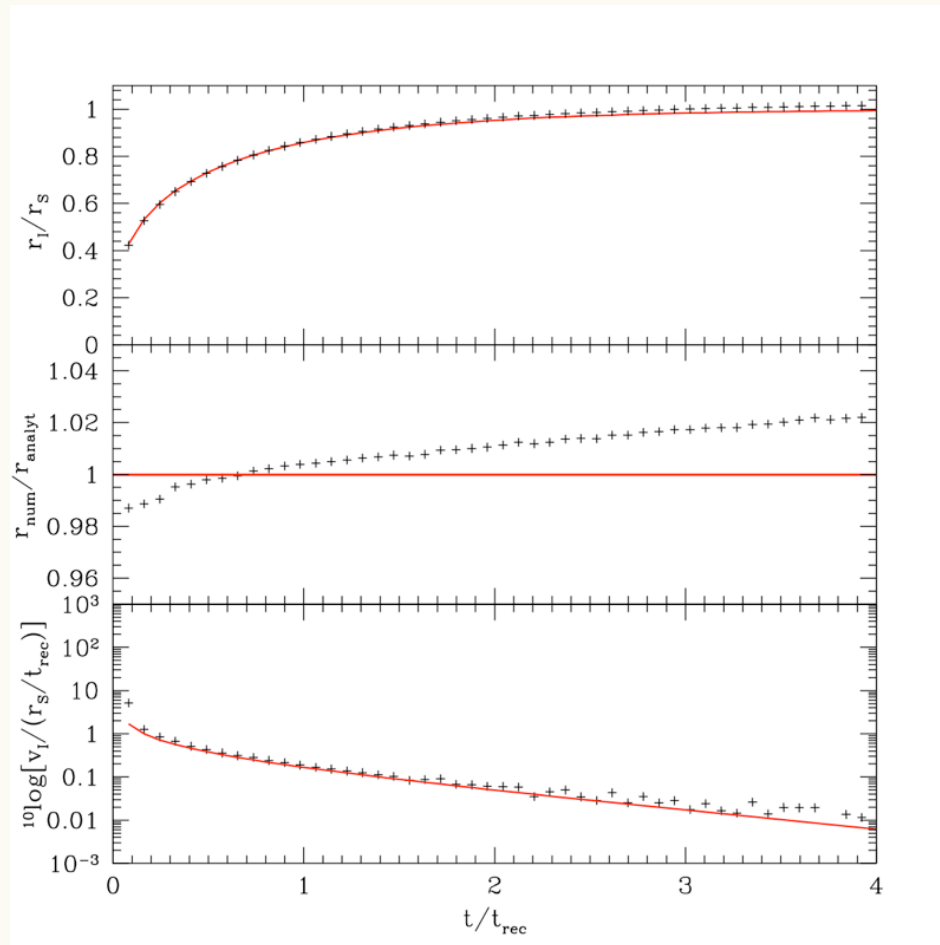


500 Myr



# Results Test 1

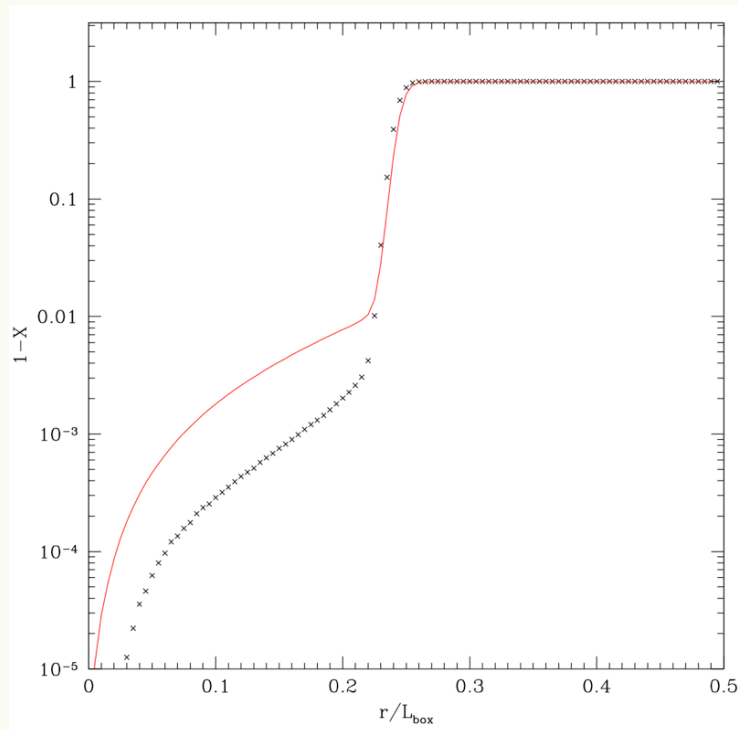
## Ionisation front position in homogeneous medium (Test 1)



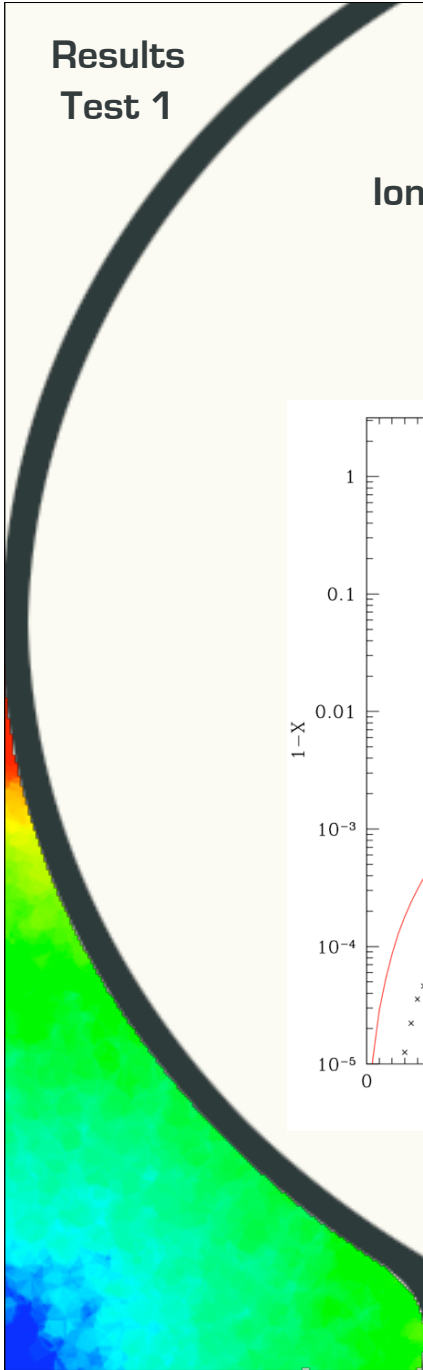
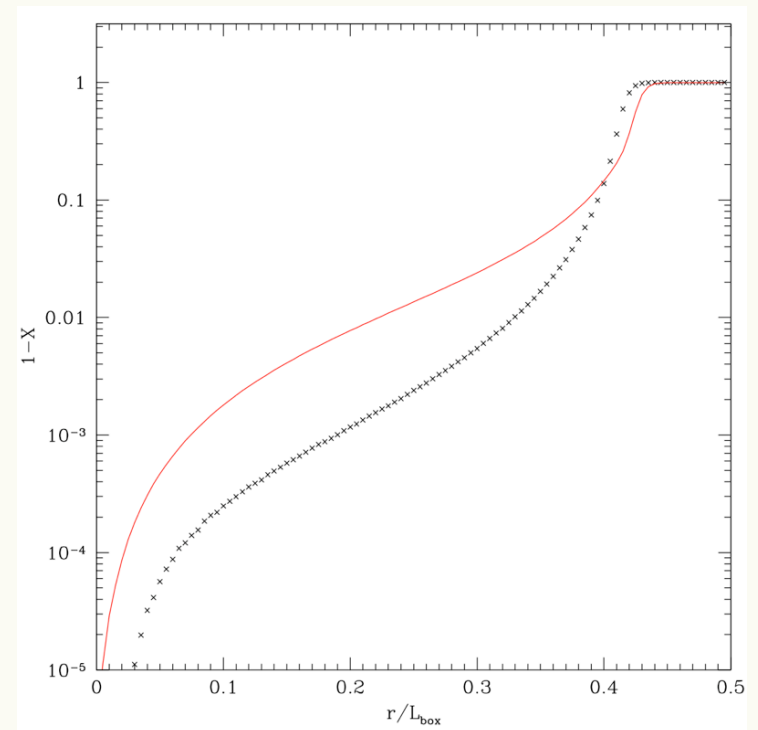
# Results Test 1

## Ionised fraction

30 Myr



500 Myr



Introduction

SimpleX

**Test 1**

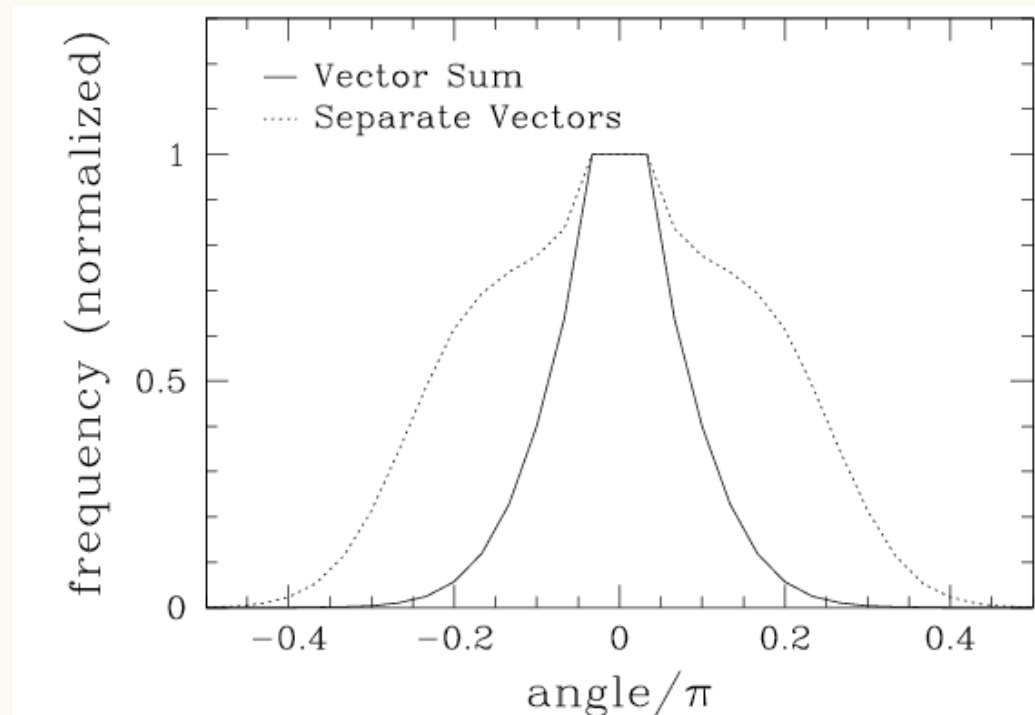
Test 4

Conclusions

# Numerical Scatter

Inner regions of Stromgren sphere have low optical depth

Numerical scatter

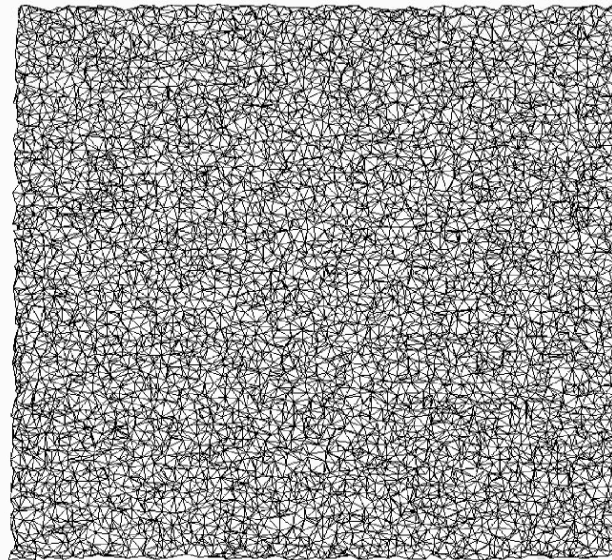


## Numerical Scatter

Origin of numerical scatter lies in changing optical depth

Grid no longer physical

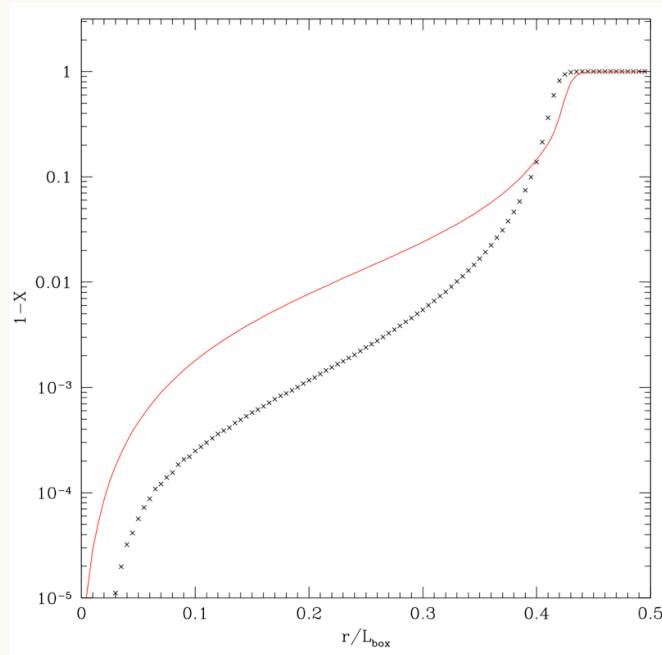
Update the grid when optical depth changes



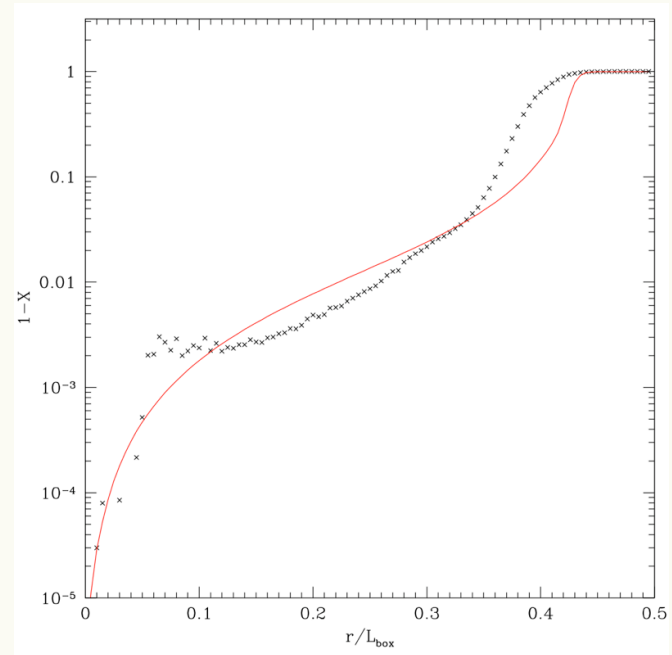


# Dynamic Updates

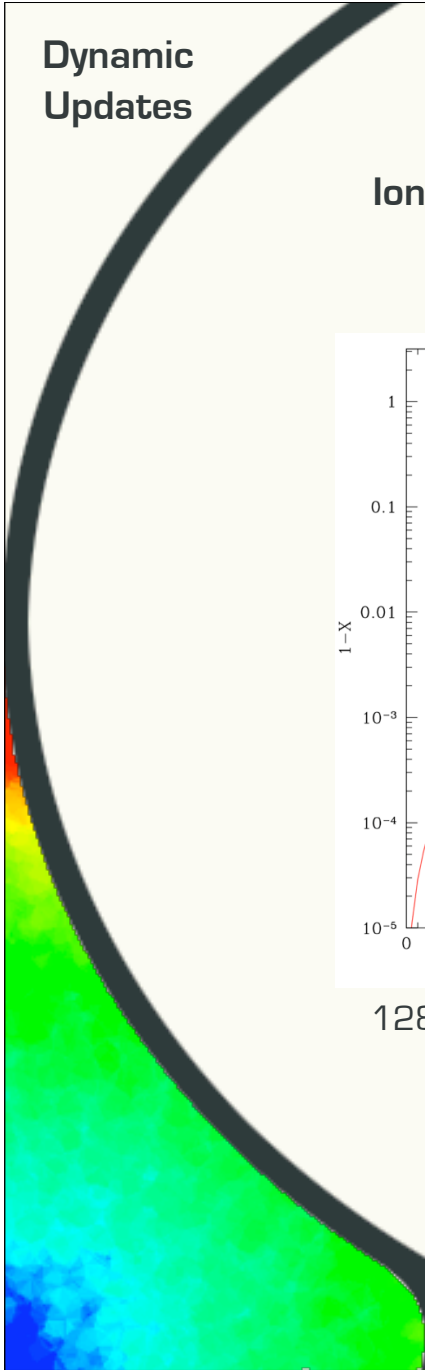
## Ionised fraction



128<sup>3</sup> no updates



80<sup>3</sup> updates

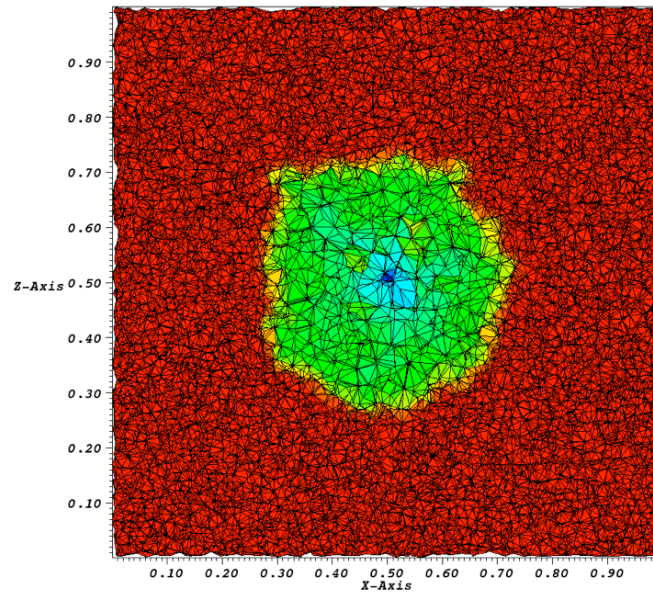


## Dynamic Updates

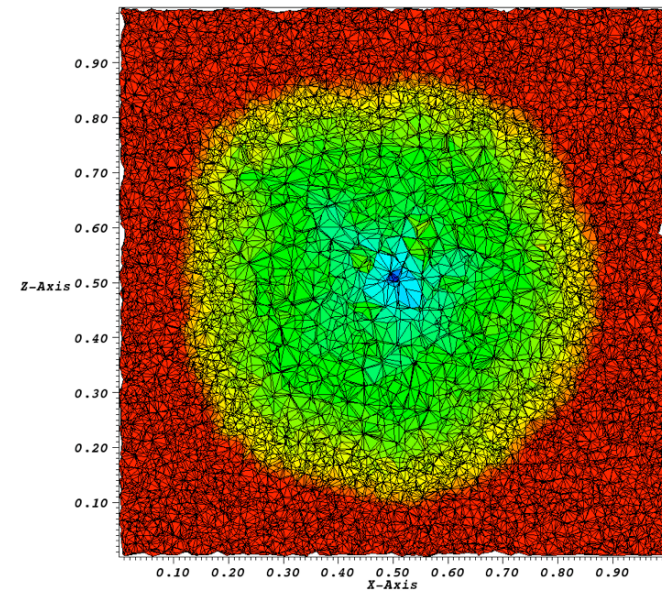
### Better results but noisy

Noisiness caused by lack of points close to source

Work in progress!



30 Myr



500 Myr

Introduction

SimpleX

**Test 1**

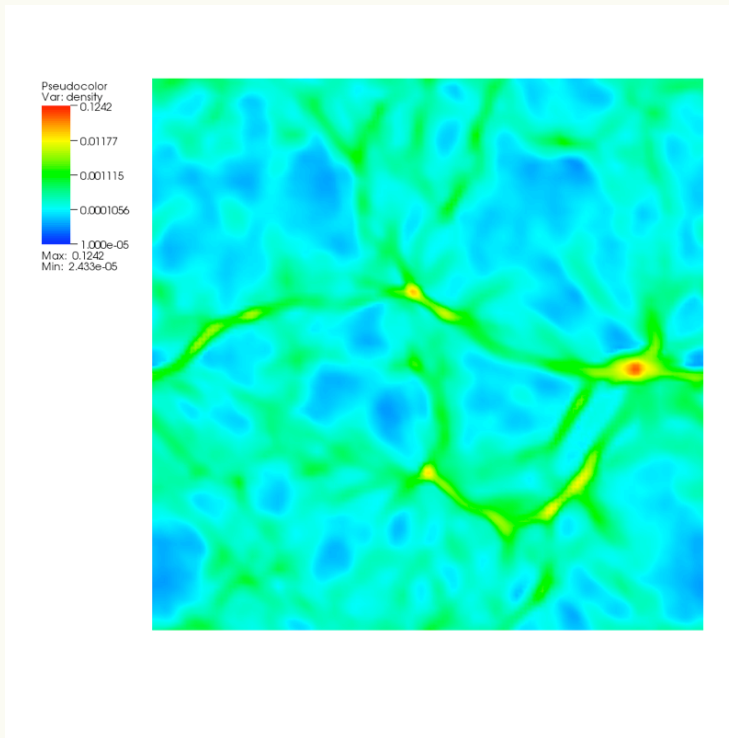
Test 4

Conclusions

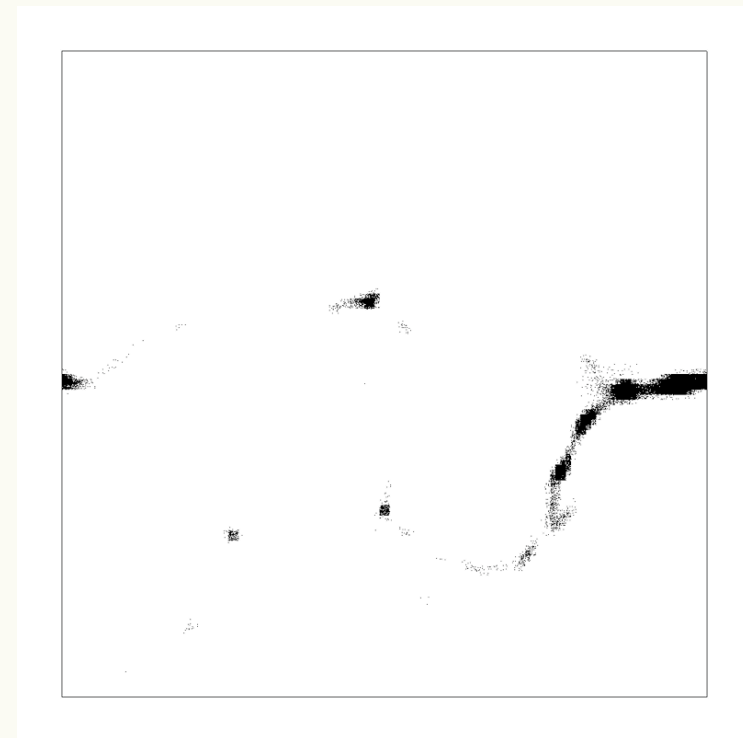
# Results Test 4

## Cosmological density field and multiple sources (Test 4)

Sampling with density<sup>3</sup> results in undersampling of lower density regions



density

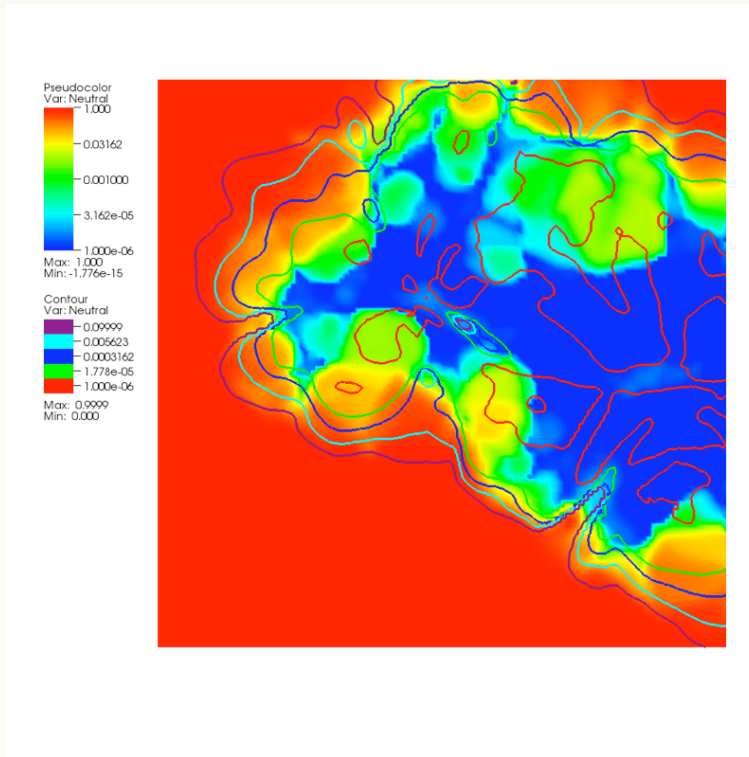


sampling

# Results Test 4

**Bad sampling gives bad results!**

Not enough directions into low density regions



Results after 0.2 Myr

sampling: density<sup>1/2</sup>

128<sup>3</sup> points

contours: C<sup>2</sup>Ray

## Sampling Function

### New sampling function

$$f(n(\vec{x})) = \left( \left( \frac{n(\vec{x})}{n_0(\vec{x})} \right)^{-3} + \left( \frac{n(\vec{x})}{n_0(\vec{x})} \right)^{-\alpha} \right)^{-1}$$

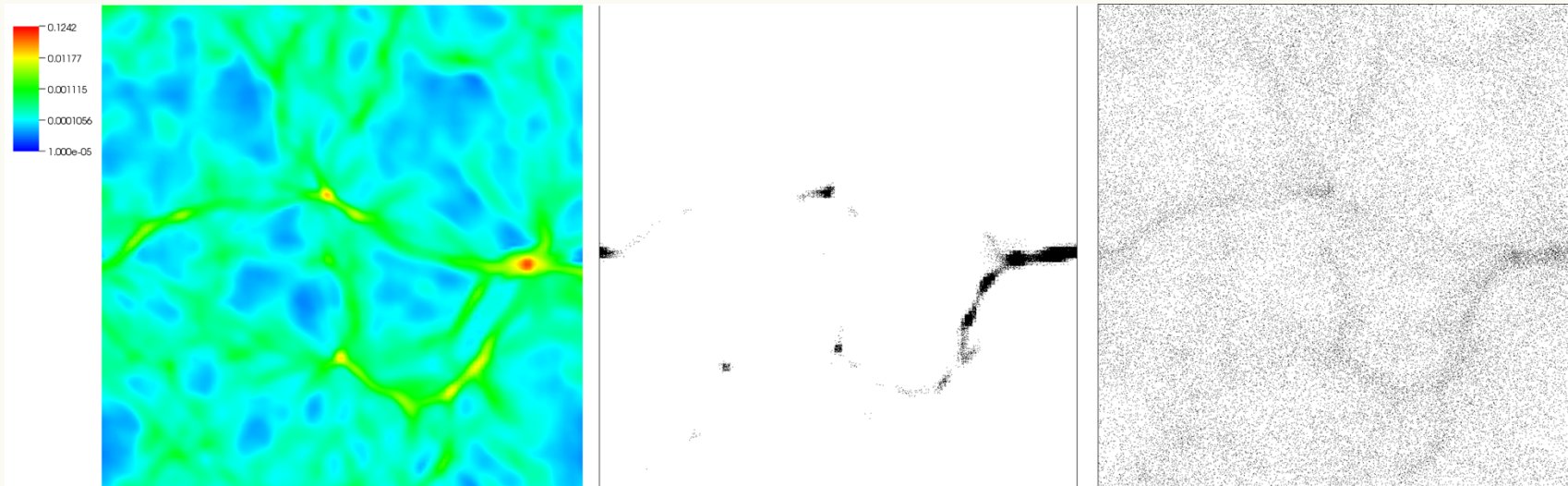
Different sampling recipe in high density regions

Change interaction coefficient accordingly

$n_0(\vec{x})$  and  $\alpha$  depend on density distribution

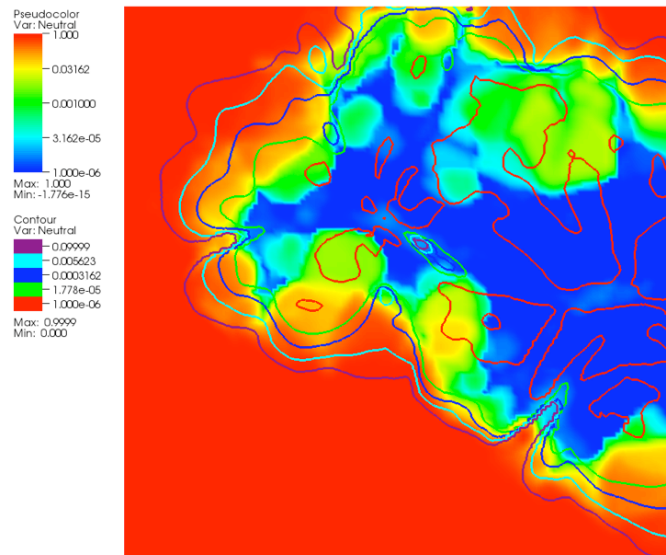
# Sampling Function

Better sampling in low density regions...

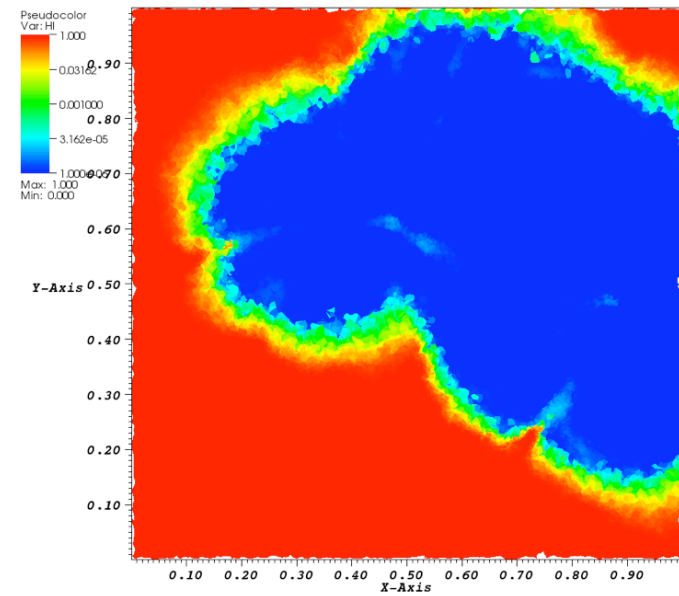


# Results Test 4

...leads to more realistic results

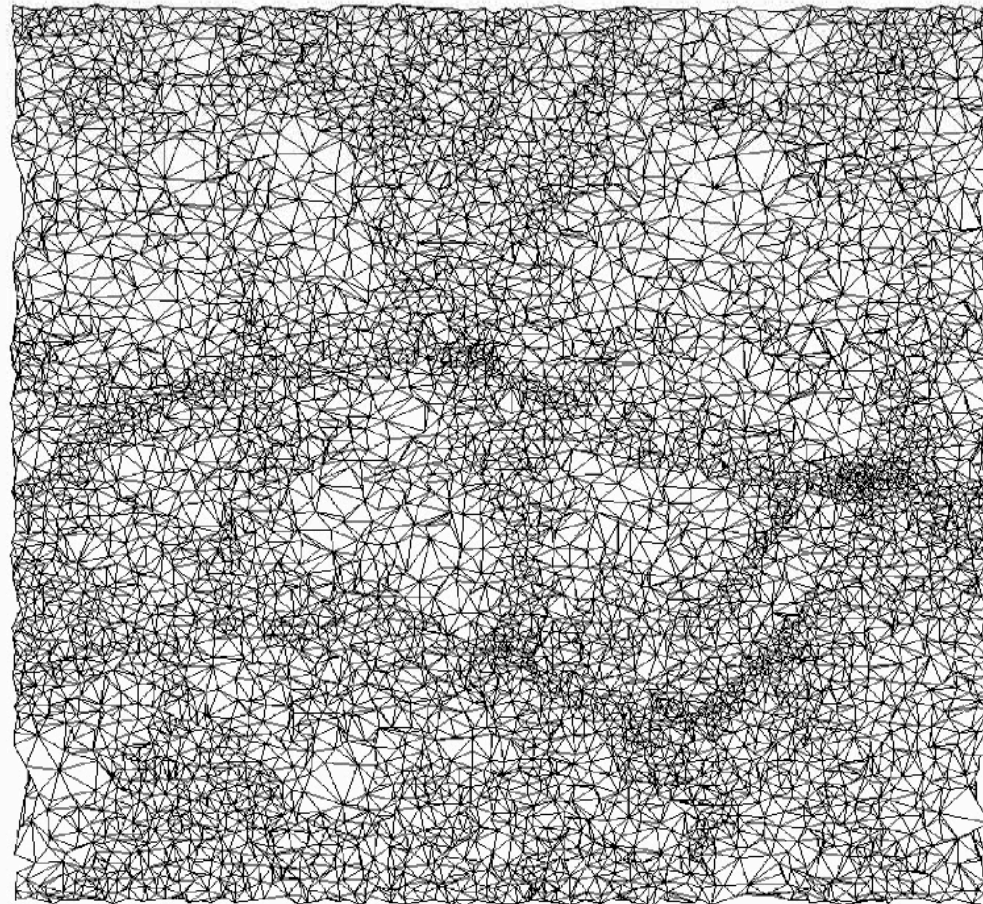
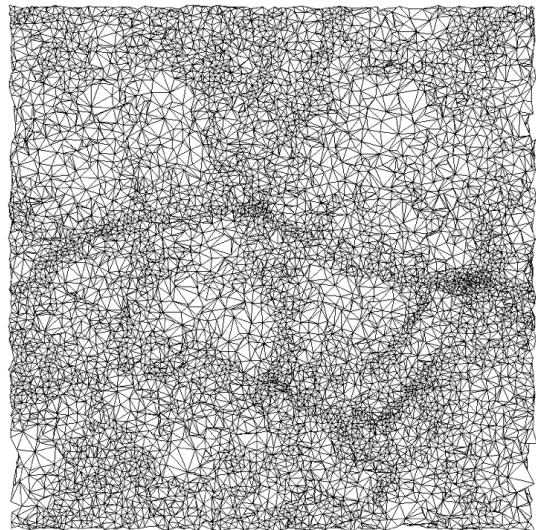


old sampling



new sampling

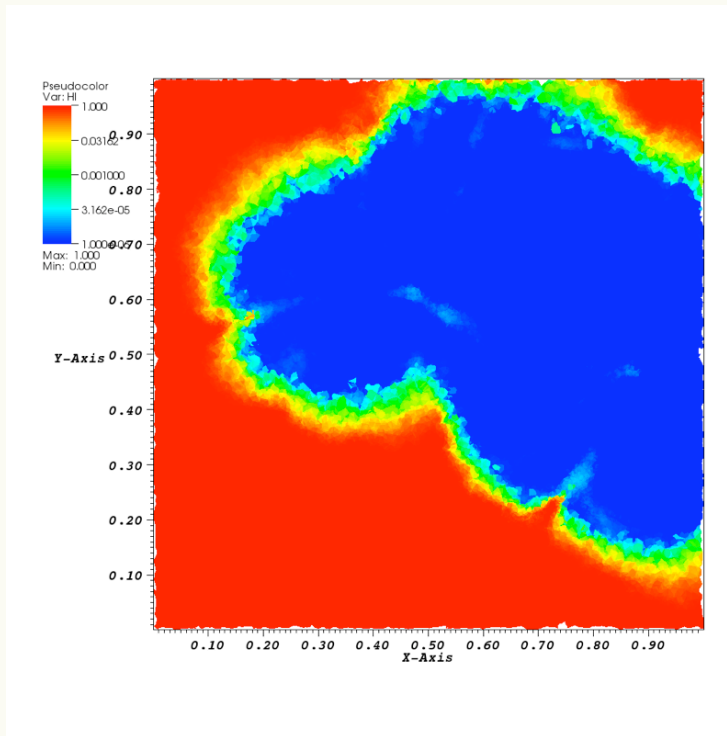
Results  
Test 4



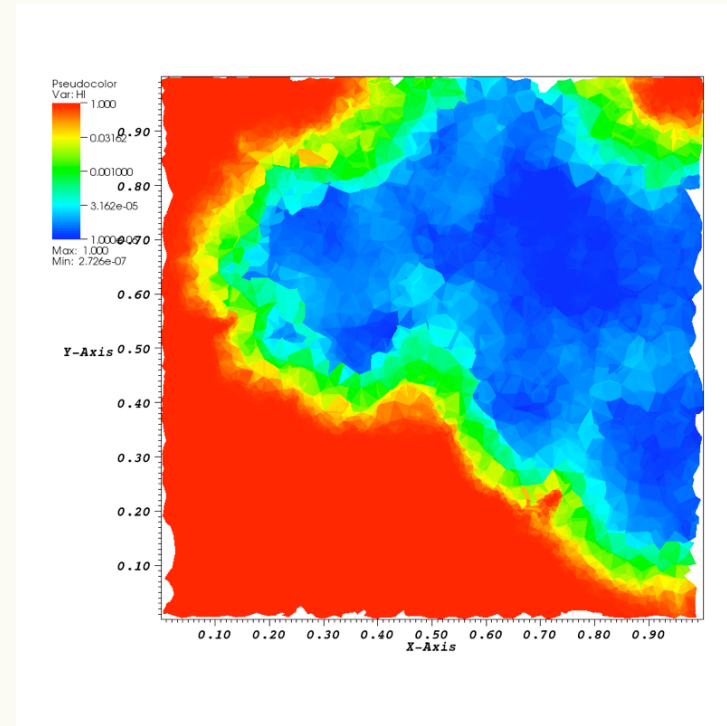


# Results Test 4

Inner structure of ionised regions shows up when grid is updated



128<sup>3</sup> no updates



80<sup>3</sup> updates

## Conclusions

### SimpleX

is computationally very efficient

does not scale with the number of sources

### The inner parts of HII region are not very well represented

updating the grid reduces the problem but also reduces resolution

other solutions are currently developed

### How severe is the problem?

Inner parts of HII region are dominated by diffuse recombination radiation  
(Ritzerveld, 2006)

