Self-Regulated Reionization and the Fluctuating H₂ Dissociating UV Background

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Simulating Cosmic Reionization at Large Scales I. : The Geometry of Reionization

Iliev, Mellema, Pen, Merz, Shapiro & Alvarez (2006) MNRAS, 369, 1625 (astro-ph/0512187)



N-body + Radiative Transfer → Reionization simulation

- N-body simulation yields the density field and sources of ionizing radiation
 - **PMFAST** code (Merz, et al. 2005) with $1624^3 = 4.28$ billion particles, 3248³ cells,

particle mass = $2.5 \times 10^7 M_{sun}$ (100 h⁻¹Mpc box),

- Halo finder "on-the-fly" yields location, mass, other properties of all galaxies,

 $M \geq 2.5 \ x \ 10^9 \ M_{sun}$ (100 $h^{\text{--1}} Mpc$ box),

e.g. $N_{halo} \sim 4 \times 10^5$ by z ~ 8 (WMAP1)

 $\sim 3 \times 10^5$ by z ~ 6 (WMAP3)

N-body + Radiative Transfer → Reionization simulation

 Radiative transfer simulations evolve the radiation field and nonequilibrium ionization state of the gas

- New, fast, efficient C²-Ray code (Conservative, Causal Ray-Tracing) (Mellema, Iliev, Alvarez, & Shapiro 2006, *New Astronomy*, 11, 374) uses shortcharacteristics to propagate radiation throughout the evolving gas density field provided by the N-body results, re-gridded to (203)³ and (406)³ cells, for different resolution runs, from each and every galaxy halo source in the box.

e.g.
$$N_{halo} \sim 4 \times 10^5$$
 by $z \sim 8$ (WMAP1)
~ 3 x 10⁵ by $z \sim 6$ (WMAP3)

Every galaxy in the simulation volume emits ionizing radiation

- We assume a constant mass-to-light ratio for simplicity:
 - $f_{\gamma} = #$ ionizing photons released by each galaxy per halo baryon $= f_* f_{esc} N_i$,

where

- f_{*} = star-forming fraction of halo baryons,
 - f_{esc} = ionizing photon escape fraction,
 - $N_i =$ # ionizing photons emitted per stellar baryon over stellar lifetime

e.g. N_i = 50,000 (top-heavy IMF), $f_* = 0.2$, $f_{esc} = 0.2 \rightarrow f_{\gamma} = 2000$

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baryon over stellar lifetime e.g. N_i = 50,000 (top-heavy IMF), $f_* = 0.2$, $f_{esc} = 0.2$ $f_{\gamma} = 2000$

• This yields source luminosity: $dN_{\gamma}/dt = f_{\gamma} M_{bary} /(\mu m_H t_*)$, $t_* = source lifetime (e.g. 2 x 10^7 yrs)$, $M_{bary} = halo baryonic mass$

Self-Regulated Reionization

Iliev, Mellema, Shapiro, & Pen (2007), MNRAS, 376, 534; (astro-ph/0607517)

Jeans-mass filtering →
 low-mass source halos
 (M < 10⁹ M_{solar}) cannot form
 inside H II regions ;

•35/h Mpc box, 406³ radiative transfer simulation, WMAP3, $f_{\gamma} = 250;$

•resolved all halos with M > 10⁸ M_{solar} (i.e. all atomically-cooling halos), (blue dots = source cells);





Extended reionization: Jeans-mass filtering, halo-mass-dependent emissivity

Cases

- 1. Halo masses $M_{solar} > 10^9$ $f_{\gamma} = 2000$ (e.g. Pop III);
- 2. Halo masses $M_{solar} > 10^9$ $f_{\gamma} = 250$ (e.g. Pop II);
- 3. Halo masses $M_{solar} > 10^8$ $f_{\gamma} = 250$ (e.g. Pop II), lower-mass halos suppressed inside H II regions (Jeans-mass filtering) ;
- 4. Same as 3., but $f_{\gamma} = 2000 (M_{solar} < 10^9)$ $f_{\gamma} = 250 (M_{solar} > 10^9)$



New, Large-Scale Simulations of Self-Regulated Reionization

Iliev, Mellema, Pen, Shapiro, and Merz (2008), in press (astroph/0806.2887);

Shapiro, Iliev, Mellema, Pen, & Merz (2008), AIPC, 1035, 68 (astro-ph/0806.3091)

CubeP³M N-body ACDM sim with 3072³ (29 billion) particles, 6144³ cells, box size = 160 Mpc; particle mass = 5 million solar masses



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CubeP³M N-body ACDM sim with 3072³ (29 billion) particles, resolves halos above 10⁸ solar masses



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CubeP³M N-body

 new Texas Sun Constellation Linux Cluster, *Ranger*, 2048 cores, 159,000 SUs (cores x hours)









ACDM Halo Mass Function (M > 10⁸ Solar Masses) from CubeP³M N-body Simulations



C²Ray radiative transfer

- RT grid 432³ cells
- box size = 90 Mpc



C²Ray radiative transfer

- RT grid 432³ cells
- box size = 90 Mpc
- *Ranger*, Texas Sun Constellation Linux Cluster, 700,000 SUs (cores x hours), up to 10,000 cores



Self-Regulated Reionization in ΛCDM



• 90 Mpc box



160 Mpc box	90 Mpc box
z = 11.6	z = 11.9
when we are the days of initial function of which are	

when mass-weighted mean ionized fraction of universe $x_m = 0.3$

Self-regulated halo mass function

- Jeans-mass filtering suppresses formation of sources in smallmass halos which form inside H II regions
- clustering of small-mass halos around density peaks enhances this effect → suppression is strongly biased



Evolution of the Mean Ionized Fraction of the Universe



Notation

• Our simulations are characterized by Low mass sources suppression 64Mpc_f100C_f250S_432 Boxsize = High mass 64/h Mpc Sources efficiency Elow mass sources efficiency RT grid = 432³

Ahn, Shapiro, Iliev, Mellema, & Pen 2008, ApJ, submitted (astro-ph/0807.2254; 0807.0920)

• Simulations suggest first stars formed inside minihalos of mass ~ 10^{5-6} solar masses at redshift z >~ 20, when H₂ molecules cooled the primordial, metal-free gas and gravitational collapse ensued.

• **But** H_2 Lyman-Werner ("LW") band photons (11.2 – 13.6 eV) dissociate H_2 , so too much LW background intensity (i.e. $J_{LW} > (J_{LW})_{threshold}$)

 \rightarrow star formation inside minihalos suppressed

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• **But** during EOR, sources of reionization also emit continuum below 13.6 eV Lyman limit, in the H₂ LW bands \rightarrow rising LW background inevitable!

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• How high does it get?

Ahn, Shapiro, Iliev, Mellema, & Pen 2008, ApJ, submitted (astro-ph/0807.2254; 0807.0920)

- Ionization sources also emit continuum below Lyman limit, in the H₂ Lyman-Werner bands (11.2 – 13.6 eV).
- In IGM, this radiation is attenuated by scattering in H Lyman series lines and downgrading to lower energy photons.
- By transfering this radiation from each source halo thru the IGM, we compute the inhomogeneous LW band intensity field durng reionization.
- e.g. Pop II sources, $f_{esc} = 0.2, f_* = 0.2,$ $f_{\gamma} = 250.$

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35/h Mpc box

Previous approximation for cosmic mean LW Background during EOR: homogeneous universe → "saw-tooth" modulation

- assume sources of UV emissivity *uniformly* distributed in space (e.g. Haiman et al. 2000; Ricotti et al. 2002; Yoshida et al. 2003)
- assume H₂ dissociating photons, emitted below H Lyman limit, are removed whenever they redshift into an H Lyman series line and are resonantly scattered by the IGM, down-converting them out of LW bands
- uniform IGM opacity filters uniformly distributed LW emitters by "saw-tooth" modulation.



(Haiman, Abel, and Rees 2000)

Attenuation of LW photons from a single source: "picket-fence" modulation

- A source at redshift z_s observed at different distances suffers different amounts of attenuation, dilution, and redshift
- When LW photon redshifts into the nearest lower H Lyman series line, it is scattered and destroyed (converted to lower energy photon).
- Source is completely attenuated at comoving distance

 $r_{cMpc} = 97 [(1 + z)/21]^{-0.5}$



LW background radiative transfer is intrinsically cosmological : sources along the "past light-cone" of every point in space

- Space-time diagram of radiation sources and observer at point P at conformal time τ
- luminosity of each halo source is constant during finite time-step
- observer at point P will see sources whose world lines intersect the past light-cone
- must determine the attenuation, dilution, and redshift of the LW photons emitted at A and received at P



comoving distance (Mpc)

 $J_{\nu}(\mathbf{x}_{obs}, z_{obs}, \nu_{obs})$ at observed frequency ν_{obs} at some comoving position \mathbf{x}_{obs} at redshift z_{obs} is given by

$$J_{\nu}(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}}) = \frac{1}{4\pi} \sum_{s} F_{\nu,s}(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}}),$$
(5)

where $F_{\nu,s}$ is the flux received at $(\mathbf{x}_{obs}, z_{obs}, \nu_{obs})$ that was emitted at $(\mathbf{x}_s, z_s, \nu_s)$ by a source (denoted by subscript s), where

$$\frac{\nu_{\rm s}}{\nu_{\rm obs}} = \frac{1+z_{\rm s}}{1+z_{\rm obs}}.$$
 (6)

The position and redshift, (\mathbf{x}_{s}, z_{s}) , of a source are related to those of the observer at $(\mathbf{x}_{obs}, z_{obs})$ by the fact that the signal emitted at the epoch z_{s} must reach the position \mathbf{x}_{obs} at the epoch z_{obs} , travelling at the speed of light while the universe expands. We express this implicitly by writing the comoving separation, r_{os} , of the source and observer as follows:

$$r_{\rm os} = |\mathbf{x}_{\rm obs} - \mathbf{x}_{\rm s}| = \int_{t(z_{\rm s})}^{t(z_{\rm obs})} \frac{cdt}{a(t)} = -\int_{z_{\rm obs}}^{z_{\rm s}} c \frac{dz}{H(z)}.$$
(7)

The differential flux, $F_{\nu,s}$, received at $(\mathbf{x}_{obs}, z_{obs}, \nu_{obs})$ from a source of differential luminosity L_{ν} emitted at $(\mathbf{x}_{s}, z_{s}, \nu_{s})$ is given by

$$F_{\nu,s}(\mathbf{x}_{\rm obs}, z_{\rm obs}, \nu_{\rm obs}) = \frac{L_{\nu} \left(\nu = \nu_{\rm s}\right)}{4\pi D_L^2(z_{\rm obs}, z_{\rm s})} \cdot \left(\frac{1+z_{\rm s}}{1+z_{\rm obs}}\right) \cdot \exp\left[-\tau_{\nu_{\rm obs}}\right],\tag{9}$$

Here $D_L(z_{\rm obs}, z_{\rm s})$ is

the luminosity distance given by

$$D_L(z_{\rm obs}, z_{\rm s}) \equiv \left(\frac{r_{\rm os}}{1+z_{\rm obs}}\right) \left(\frac{1+z_{\rm s}}{1+z_{\rm obs}}\right),\tag{10}$$

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Expected number of computational operations : ~ N_{sources} * N_{cells} * N_{frequencies} where N_{sources} >~ 10⁷ within the LW horizon of r_{LW} ~ 100 cMpc N_{cells} >~ 10⁶ grid cells for sufficient resolution and statistical accuracy N_{frequencies} >> 1 for multi-frequency transfer of optically thick Lyman series lines
 → full 3D, multi-frequency radiative transfer would be prohibitive!!

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→ *full 3D*, *multi-frequency radiative transfer would be prohibitive!!*→ We solve this by making a grey opacity approximation equivalent to multi-frequency...

Attenuation of LW photons from a single source: "picket-fence" modulation factor



Modulation Factor

LW background radiative transfer is intrinsically cosmological : sources along the "past light-cone" of every point in space

- Space-time diagram of radiation sources and observer at point P at conformal time τ
- luminosity of each halo source is constant during finite time-step
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comoving distance (Mpc)

Ahn, Shapiro, Iliev, Mellema, & Pen 2008, MNRAS, submitted (astro-ph/0807.0920)

- LW background radiative transfer code parallelized using MPI for distributedmemory parallel computers;
- e.g. 35/h Mpc reionization simulation has $(203)^3$ cells, $N_{sources} = 200,000$ by z = 8, but must do LW transfer in 5³ boxes stacked around the central box to fill 100 Mpc LW horizon \rightarrow $N_{sources}$, total > 20 million!
- Ran for 22 hours, on 320 computing cores, 1.5 GB memory per core, Texas supercomputer *Lonestar* (5200 cores of dual-core Intel Xeon processors, with 11.6 TB aggregate memory).



35/h Mpc box

H₂ Dissociating Background during EOR



H₂ Dissociating Background during EOR





The Mean H₂ Dissociating UV Background During EOR



 $J_{LW, 21} = J/(10^{-21} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ Hz}^{-1} \text{ ster}^{-1})$

Distribution of Intensity Fluctuations for the LW Background During Reionization



(35/h Mpc box)

What are the dominant sources of the LW background during the EOR?

- Self-regulation of reionization
 - → early LW background is dominated by lowmass sources that are suppressed if they form inside H II regions,
 - BUT the rise of the small-mass sources saturates long before end of EOR

→

the high-mass sources eventually dominate the LW background



LW background intensity fluctuations in space are correlated with matter density fluctuations

z = 19



z = 13

LW Background Conclusions

- Picket-fence modulation of LW background photons
 - makes computation of inhomogeneous LW background tractable
- LW rises above the threshold for suppressing star formation in minihalos long before end of the EOR → supports the idea that MHs, on average, not significant reionization source, but
- LW intensity fluctuates significantly in space → may be "safe spots" early on, to form Pop III stars in minihalos where LW background minima occur, far from the large-scale H II regions made by clustered dwarf galaxies.
- Fluctuation in LW background comes from source clustering, at a scale of ~10 comoving Mpc
- May contribute to NIR background fluctuations
- Understanding radiative feedback on Pop III star formation in minihalos may be important to complete the theory of reionization

More Feedback From First Radiation Sources: H⁻ Photodissociation

Chuzhoy, Kuhlen, & Shapiro (2007), ApJL, 665, L85 (astro-ph/0704.0426)

• Rate for H_2 formation in primordial gas,

 $H^- + H \rightarrow H_2 + e^-$

is proportional to abundance of $H^- ==>$ destroying H^- will reduce H_2 formation rate;

• Photodissociation can destroy H⁻,

 $H^- + \gamma \rightarrow H + e^-$ ($\nu \ge 0.755 \text{ eV}$);

• During reionization, as sources release ionizing radiation, they also cause a background of H⁻ dissociating radiation to build up, which reduces the H_2 formation rate by factor F_s ,

 $F_{s} \sim 1 + 1000 k_{s} x / (f_{esc} \delta)$,

where x = cosmic mean ionized fraction, δ = local baryon gas overdensity,
and k_s = a constant of order unity which depends on type of radiation source
(e.g. recombination radiation, direct stellar or quasar emission, or secondary emission
by nonthermal electrons following X-ray background ionization);

• Hence, by the time $x \ge 0.1$, H⁻ photodissociation may significantly reduce H₂ abundance and cooling, and the rate of primordial star formation.