

How long would the Sun shine?

- The Sun needs fuel to shine.
 - The Sun shines by consuming the fuel -- it generates energy from the fuel.
- The lifetime of the Sun is determined by
 - How fast the Sun consumes the fuel, and
 - How much fuel the Sun contains.
- How fast does the Sun consume the fuel?
 - Energy radiated per second is called the “*luminosity*”, which is in units of watts.
 - The solar luminosity is about 3.8×10^{26} Watts.
 - Watts = Joules per second
 - Compare it with a light bulb!
- What is the fuel??

Fuel = Gravitational Energy?

- The mass of the Sun is $M = 2 \times 10^{30}$ kg.
 - The amount of the fuel should be related to the amount of mass.
- Gravity can generate energy.
 - A falling body acquires velocity from gravity.
 - **Gravitational energy = $(3/5)GM^2/R$**
 - The radius of the Sun: $R = 700$ million m
 - **Gravitational energy of the Sun = 2.3×10^{41} Joules.**
- How long could the Sun shine on gravitational energy?
 - Lifetime = (Amount of Fuel)/(How Fast the Fuel is Consumed)
 - Lifetime = $(2.3 \times 10^{41} \text{ Joules}) / (3.8 \times 10^{26} \text{ Joules per second}) = 0.6 \times 10^{15}$ seconds.
 - Therefore, the Sun lasts for **20 million years** (Helmholtz in 1854; Kelvin in 1887), if gravity is the fuel.

Fuel = Nuclear Energy

- Einstein's Energy Formula: $E=Mc^2$
 - The mass itself can be the source of energy.
- If the Sun could convert *all* of its mass into energy by $E=Mc^2$...
 - Mass energy = 1.8×10^{47} Joules.
 - Compare it with the gravitational energy, 2.3×10^{41} Joules, which can keep the Sun shining for 20 million years.
 - The Sun would shine for about **15 trillion years** on mass energy!
- How can the mass be converted into energy?
 - Nuclear reaction
 - Nuclear reaction in the Sun can convert ~0.07% of the mass into energy.
- Therefore, the Sun shines for...
 - $15 \text{ trillion years} \times 0.0007 \sim \mathbf{10 \text{ billion years}}$

Burning Hydrogen: p-p chain

- ${}^1\text{H} + {}^1\text{H} \rightarrow {}^2\text{H} + e^+ + \nu_e$
- ${}^2\text{H} + {}^1\text{H} \rightarrow {}^3\text{He} + \gamma$
- ${}^3\text{He} + {}^3\text{He} \rightarrow {}^4\text{He} + {}^1\text{H} + {}^1\text{H}$
 - ${}^1\text{H}$: proton, ${}^2\text{H}$: deuteron
 - ${}^3\text{He}$: Helium-3, ${}^4\text{He}$: Helium-4
 - e^+ : positron, ν_e : neutrino, γ : gamma ray
- In total, four protons are fused into one helium-4 and produce energy:
 - ${}^1\text{H} + {}^1\text{H} + {}^1\text{H} + {}^1\text{H} \rightarrow {}^4\text{He} + \text{“binding energy”}$
 - One proton weighs 1.6726×10^{-27} kg
 - One helium-4 weighs 6.643×10^{-27} kg
 - Four protons minus one helium = 4.7×10^{-29} kg \rightarrow energy
 - This is 0.7% of the original mass of four protons.

How Hot is the Sun?

- Hydrogen gas is pulled inward by gravity.
- **Hydrogen Gas is pushed outward by pressure.**
 - Nuclear energy heats up gas \rightarrow high pressure
 - $\text{Pressure} = k_B \times (\text{number density of hydrogen}) \times (\text{temperature})$
 - Pressure is the highest at the center and decreases at larger distances.
- “Hydrostatic equilibrium” = “Pressure force balances gravitational force”
 - Gravity = GM^2/R^2
 - Pressure = $k_B nT$
 - Calculations show that temperature should be $\sim 20 \text{ million K}$
 - High temperature is necessary to balance enormous gravity.

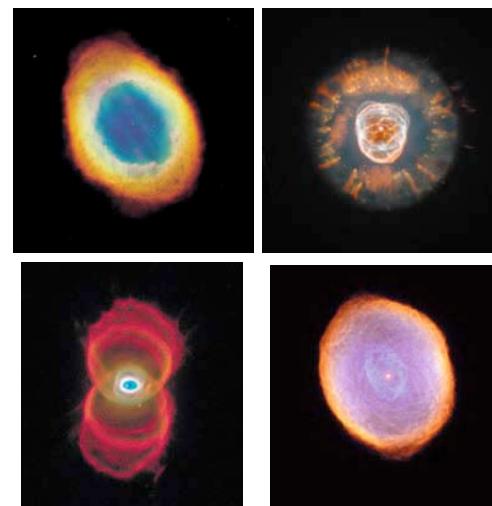
Core is Hotter, Surface is Cooler

- **Core** ($0-0.25 R_{\text{solar}}$): ~ 15 million K
 - Energy is produced by hydrogen burning
- **Radiative zone** ($0.25-0.70 R_{\text{solar}}$): 2 to 8 million K
 - Energy is carried by radiation (photons) up to near the surface of the Sun
 - Photons frequently scattered by electrons (random walk)
- **Convective zone** ($0.70-1 R_{\text{solar}}$): < 2 million K
 - Photons are absorbed by atoms near the surface; unable to carry energy
 - Energy is then carried by “convection” (e.g., boiled water)
- **Surface:** 5,800 K
 - It takes about a million years from the core to the surface.

Fate of the Sun

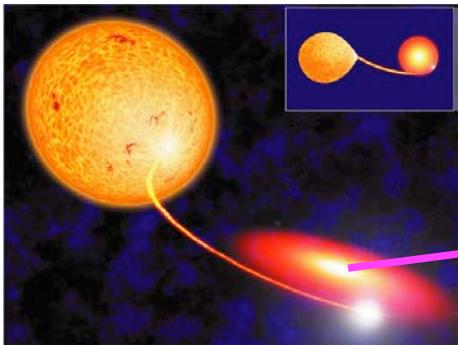
- The Sun will eventually run out of fuel...
 - The Sun is about 5 billion years old.
 - Hydrogen burning can keep the Sun shining for about 10 billion years.
- What would happen after that?
 - The Sun will find another source of fuel: **Helium**
- When hydrogen nuclei are exhausted, the Sun begins to contract, getting hotter.
- When temperature in the core increases to ~ 100 million K, helium begins to burn, generating nuclear energy again. The surface of the star expands.
 - ${}^4\text{He} + {}^4\text{He} + {}^4\text{He} \rightarrow {}^{12}\text{C} + (\text{binding energy})$
- When helium nuclei are exhausted, the star wants to burn carbon, but a low-mass star can't burn it...
 - ${}^{12}\text{C} + {}^4\text{He} \rightarrow {}^{16}\text{O} + (\text{binding energy})$; this reaction requires ~ 600 million K!
So, a low-mass star becomes a carbon star.

White Dwarfs and Planetary Nebulae



- Expanding gas gets **ionized** by radiation from the central core
- The carbon core became a “White Dwarf”
 - Supported by “degeneracy pressure”
- The expanding gas
 - Planetary nebula

Type Ia Supernovae



- If the W.D. has a companion star, mass from the companion accretes on the W.D., increasing mass.
- At some point ($M > 1.4M_{\text{solar}}$), carbon begins to burn!
 - The “carbon bomb” disrupts the W.D. completely
 - This type of supernova is called the “Type Ia”, and plays a very important role in cosmology

Importance of Type Ia in Cosmology



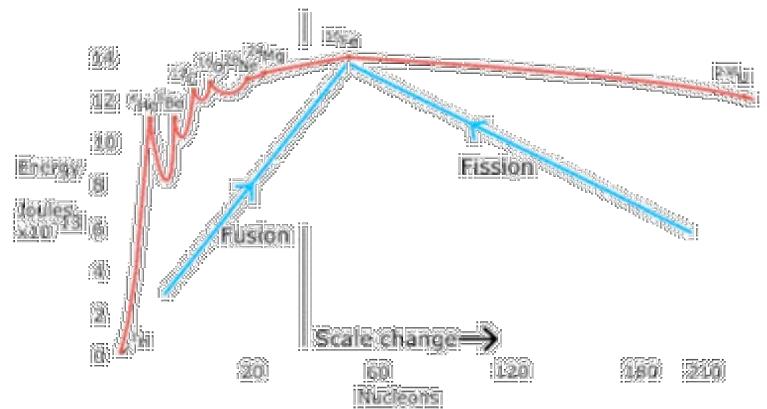
Type Ia supernova

- We can estimate distances to Type Ia supernovae fairly accurately.
 - Because they all explode at the same mass ($\sim 1.44M_{\text{solar}}$), their luminosity is roughly the same for all Type Ia.
 - We measure their brightness.
 - We know their luminosity.
 - Luminosity-brightness relation gives distances.
- Distance-redshift relation** is one of the fundamental cosmological probes.
- How do we find Type Ia?
 - No hydrogen line should be seen for Type Ia

What about Type II?

- $M > 2M_{\text{solar}}$
 - More mass, more gravity \rightarrow More pressure, higher temperature
 - Hydrogen and helium are much more rapidly consumed (\sim a few 100,000 years or less vs billions of years)
 - Then, **carbon does fuse!!** (E.g., $^{12}\text{C} + ^4\text{He} \rightarrow ^{16}\text{O}$)
 - Heavier elements are also burned one after another.
 - E.g., $^{16}\text{O} + ^4\text{He} \rightarrow ^{20}\text{Ne}$, $^{20}\text{Ne} + ^4\text{He} \rightarrow ^{24}\text{Mg}$
 - E.g., $^{12}\text{C} + ^{16}\text{O} \rightarrow ^{28}\text{Si}$, $^{28}\text{Si} + ^{28}\text{Si} \rightarrow ^{56}\text{Fe}$
 - Iron (^{56}Fe) is the terminal:** no more energy gain by fusion.
 - The core keeps shrinking... Gravitational force is not balanced by thermal pressure... Where would the gravitational energy go...
 - Type II Supernova!!** (Hydrogen lines should be seen.)
- Intermediate mass stars ($8M_{\text{solar}} > M > 2M_{\text{solar}}$)
 - The core becomes a *neutron star* (\sim 10km across; rapidly rotating)
- Very high mass stars ($M > 8M_{\text{solar}}$)
 - The core collapses into a *black hole*

Binding Energy Diagram



- Fusion generates energy until it reaches the “iron peak”.
- Fission generates energy by destroying nuclei heavier than iron.

Life and Low- and High-mass Stars

- Low-mass stars are necessary for life because...
 - Planets can form around low mass stars
 - Stars live long enough (~billions of years) for complex form of life to emerge
- High-mass stars are necessary for life because...
 - Low-mass stars alone cannot produce important heavy elements such as carbon, oxygen, nitrogen, etc.
 - High-mass stars can create heavy elements by fusion, and eject the created elements into space by Type II supernova explosion.
- Life is not possible without both!