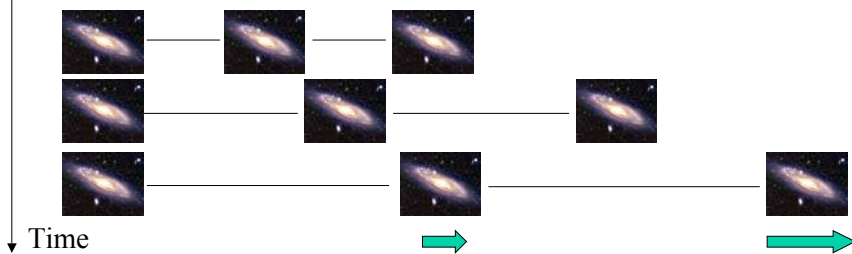


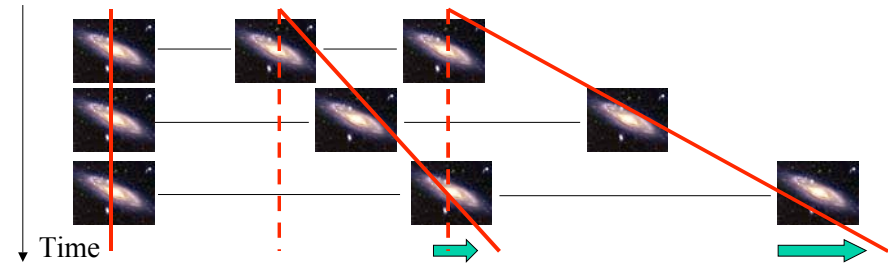
Expansion of the Universe

- The universe is expanding.
 - General relativity: space is dynamical and expanding.
 - Distance between galaxies increases with time
 - But there is important exception.
- $L = R l$
 - L : actual distance (which increases with time)
 - R : **scale factor** (which represents the size of the universe and increases with time)
 - l : “comoving” distance (which is independent of time)



Comoving Coordinate

- Galaxies are **not** moving!
 - It is space between galaxies that is expanding.
 - (But there is peculiar motion which we have ignored so far)
- “Comoving coordinate” is the coordinate which expands in the same way as space.
 - Therefore, galaxies always remain at the same position in comoving coordinates.



Velocity-distance Law

- Galaxies appear to be moving away from us.
 - Recession velocity of galaxies represents expansion velocity of space
- $L = R l$
 - Recession velocity V
 - = rate of increase of L
 - = (rate of increase of R) \times l
 - = (rate of increase of R)/ $R \times L$
 - = $H L$
 - More distant galaxies recede faster.
 - But, this does not mean that we are at the center of the universe.



Discovery of the expansion of the universe

- How do we confirm the velocity-distance law?
 - We need recession velocities of galaxies: V
 - We need distances to galaxies: L
- How do we measure V ?
 - Use Doppler shifts: $V = c z$ (z is “redshift”)
- How do we measure L ?
 - There are various ways to estimate distances --- this is the most difficult part.
- Edwin Hubble (1889-1953) has done this and discovered expansion of the universe in 1929!



Expansion Rate

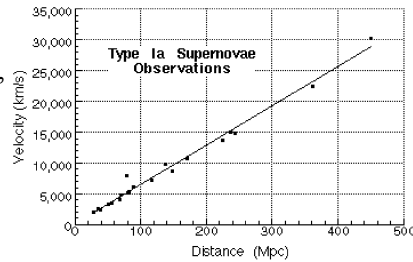
- $V = HL$

- H is the expansion rate, and is called “Hubble’s parameter”
- H has to be determined observationally.

- The latest determination:

- $H = 70$ km/s/megaparsec, or
- $H = 21.5$ km/s/million light years
- Therefore, a galaxy at 100 million light-years away appears to move away from us at 2150 km/s.
- A galaxy at 1 billion light-years away appears to move away from us at 21500 km/s (about 7% of the speed of light)

- Galaxies at 14 billion light-years away appear to move away from us at the speed of light!



Is there something wrong here?

- Galaxies at 14 billion light-years away recede at the speed of light.
 - Even more distant galaxies recede faster than the speed of light!
- Is this in accord with relativity?
 - The answer is yes.
 - If galaxies were moving faster than the speed of light, it would be in conflict with relativity; however, *galaxies are not moving!* It is space that is expanding.
 - Also, we cannot see galaxies receding faster than the speed of light because light does not reach us: **Horizon**